DISTRIBUTED PARALLEL PROCESSING AND DYNAMIC LOAD BALANCING TECHNIQUES FOR MULTIDISCIPLINARY HIGH SPEED AIRCRAFT DESIGN

by

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(ABSTRACT)

Multidisciplinary design optimization (MDO) for large-scale engineering problems poses many challenges (e.g., the design of an efficient concurrent paradigm for global optimization based on disciplinary analyses, expensive computations over vast data sets, etc.) This work focuses on the application of distributed schemes for massively parallel architectures to MDO problems, as a tool for reducing computation time and solving larger problems. The specific problem considered here is configuration optimization of a high speed civil transport (HSCT), and the efficient parallelization of the embedded paradigm for reasonable design space identification. Two distributed dynamic load balancing techniques (random polling and global round robin with message combining) and two necessary termination detection schemes (global task count and token passing) were implemented and evaluated in terms of effectiveness and scalability to large problem sizes and a thousand processors. The effect of certain parameters on execution time was also inspected. Empirical results demonstrated stable performance and effectiveness for all schemes, and the parametric study showed that the selected algorithmic parameters have a negligible effect on performance.

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1. INTRODUCTION.

The requirement for timely deliverance, in the context of inherent computational complexity and huge problem size spanning several disciplines, is typical of modern large-scale engineering problems (e.g., aircraft design). This has provided the driving force for research in the area of multidisciplinary design optimization (MDO) to develop practical, scalable methodologies for design optimization and analysis from the perspective of more than one discipline. The computational intensity of realistic multidisciplinary design optimization problems presents a major obstacle and bottleneck. For this reason, high performance computing and its efficient use constitute a very important MDO tool. There is an ongoing effort amongst engineering and scientific computing researchers to build sophisticated parallel and distributed algorithms for the solutions of specific types of problems, such as computational fluid dynamics (CFD), partial differential equations (PDEs), finite element analysis, etc. (see, for example, the July 1998 issue of *Advances in Engineering Software*). Despite their good performance and promising potential, such codes are not widely integrated in MDO environments, since it is a nontrivial task to efficiently blend heterogeneous, disciplinary engineering codes together. Obstacles that arise are complex interactions between disciplines, incompatible interfaces, nonstandard programming practices, lack of detailed documentation, and sometimes failure to scale up to the sizes of realistic MDO problems. As a result, more customization is needed than is feasible. Burgee et al. [7] discuss similar difficulties in their effort to parallelize sequential MDO codes composed of legacy disciplinary analysis codes.

Several efforts are described in the literature that propose parallel and distributed solutions to the complexity and computational burden of large scale MDO problems. One strain of research develops methodologies for MDO problem modeling and formulation with the goal of creating significant opportunities for distributed and parallel computation. Kroo et al. [24] propose two such methodologies. One is the decomposition of analyses into simpler modules with limited interdependencies, so that each module can be run concurrently. Collaborative optimization [5], on the other hand, aims at modeling the entire design process as a collaboration between parallel tasks/disciplines, under the auspices of

a centralized coordinating process. Dennis and Lewis introduce the "individual discipline feasible" [8] problem formulation approach for MDO that has the advantage of using third party disciplinary analysis codes. There is work at Georgia Tech on agent based technologies for the IMAGE infrastructure of their decision support integrated product and process development (IPPD) architecture DREAMS [15]. The applicability and scalability of the above methods for large-scale systems has yet to be established.

A second strain of research is oriented towards the design and implementation of generic MDO computing frameworks that support concurrent execution across distributed, heterogeneous platforms (see Access Manager [27], COMETBOARDS [18], and Fido [34]). For example, Wujek et al. [35] propose a framework, later extended by Yoder and Brockman [36], that facilitates distributed collaborative design [24] and manages the entire problem-solving life-cycle through a graphical user interface. These systems aim to automate the design optimization process by controlling computing processes, and tracking and monitoring intermediate results. Their problem definition capabilities need to be very flexible and robust in order to accommodate complex MDO problems. Additionally, tracking and monitoring tools like FIDO's Spy [34] are very important to keep the designer informed about the state of the optimization, and to allow the designer to interact with the automated process. Currently, more empirical evidence is needed to show if automated, "push-button" (see Dennis and Lewis [8]) systems are well suited to large, complex MDO problems.

Finally, there has been research on using sophisticated parallel algorithms for different MDO subproblems such as optimization, analysis, etc. For example, Burgee et al. [7] and Balabanov et al. [1] implemented coarse-grained parallel versions of existing analysis and optimization codes for a High Speed Civil Transport. The results were reasonable, but speedup tapered off for less than 100 nodes, due to I/O overhead, and other factors discussed in [7], [1]. Their conclusion was that fine-grained parallelism and reduced I/O versions of the codes would improve scalability. There are some reports of efficiency achieved on massively parallel architectures, i.e., scalability to thousands of nodes. For example, Dennis and Torczon [9] developed the parallel direct search methods for derivative free optimization that are blatantly parallel. Direct search methods are suitable for problems with a relatively small number

of design variables (< 50). Ghattas and Orozco have developed a parallel reduced Hessian sequential quadratic programming (SQP) method for shape optimization [12] that scales very well up to thousands (16000) of processors for relatively small numbers of design variables (< 50), but performance quickly degrades as the number of design variables increases. Eldred et al. [11] have developed an object oriented software framework for generic optimization that experienced optimal performance at 512 processors for a certain test problem, but started degrading after that. More research seems to focus on moderate parallelism, i.e., less than 100 processors. For example, Jameson et al. [20] assess parallel implementations of an algorithm applying control theory to CFD aerodynamic optimization. Reported efficiencies range between 66 and 95 percent, but the need for more effective load balancing is recognized and the focus of current study. For more research on parallel and distributed MDO tools, including parallel genetic algorithms using MPI [31], and Java based solutions, see [19], [3], [10], [2].

This paper focuses on the effective use of massive parallelism and scalable distributed control applied to the reasonable design space identification paradigm embedded within the problem of the multidisciplinary configuration optimization of a High Speed Civil Transport (HSCT). The approach here uses a variable complexity paradigm [7] where computationally cheap low fidelity techniques are used together with computationally expensive high fidelity techniques throughout the optimization process. Geometric constraints and low fidelity analysis are applied to define promising regions in the design space and to identify intervening/important variables/terms for surrogate models. Higher fidelity analyses are used to generate smooth response surfaces for those regions, which are then analyzed by the optimizers in search of local optima. Typical configuration designs are comprised of 5 to 50 design variables.

The paradigm of reasonable design space identification consists of performing millions of low fidelity analyses at extreme points of a box around a nominal configuration. A single design evaluation takes a fraction of a second on a slow processor, but as the number of design variables grows, millions of evaluations require a significant amount of time. Such an evaluation is too fine grained to lend itself to task parallelism, and so is taken as the

atomic grain of computation. In terms of data parallelism, the problem is irregular because each configuration that fails preliminary analysis (violates feasibility constraints) has to be moved towards the center of the box until it is coerced to a reasonable design. This results in a variable number of analyses and time per configuration. Initially, a parallel implementation was developed where all configurations to be evaluated were spread evenly across available processors. A severe load imbalance, where total idle time amounted to one half of total processing time, was observed. Thus dynamic load balancing strategies, so that the load can be effectively redistributed amongst processors at run time, are essential. Two receiver initiated distributed load balancing algorithms—random polling (RP) and global round robin with message combining (GRR-MC)—were implemented.

Load balancing causes remapping of jobs to processors so that processors that have finished their work at some point in time can resume with a new load. Thus a processor having no load at a certain point in time does not signify that there is no more work to be done on a global level. A termination detection algorithm is needed to assert global termination of the system. Two complementary termination detection schemes—global task count (GTC) and token passing (TP)—have been implemented. The parallel codes make use of the Message Passing Protocol (MPI) [31] for interprocessor and collective communication, and POSIX threads (pthreads) for concurrency at the processor level. To provide context, the HSCT aircraft design problem is described in detail in Chapter 2. Chapter 3 describes the reasonable design space paradigm, Chapters 4 and 5 the algorithms and their implementation. Chapters 6 and 7 analyze the results and parametric studies, and Chapter 8 offers conclusions and possible future work.

2. HSCT CONFIGURATION OPTIMIZATION.

The parallelization techniques described in the following chapters are applied in the context of designing an optimal supersonic aircraft with a capacity for 251 passengers, minimum range of 5,500 nautical miles, cruise speed of Mach 2.4, and ceiling height of 70,000 ft. The problem is formulated as a constrained optimization

$$\min_{x_{min} \leq x \leq x_{max}} f(x), \quad \text{subject to} \quad g_i(x) \leq 0 \quad \text{for all } i \in \{1, \ldots, m\},$$

where $f : \mathbf{R^n} \rightarrow \mathbf{R}$ is the objective function, $x \in \mathbf{R^n}$ is a vector of n design variables, and $g : \mathbf{R^n} \rightarrow \mathbf{R}$ is a vector of m constraints. The values of the design variables in vector x are lower and upper bounded by x_{min} and x_{max} respectively.

Takeoff gross weight (TOGW), expressed as the aggregate of payload, fuel, structural and nonstructural weights, serves as the selected objective function. TOGW is dependent on many of the engineering disciplines involved, (e.g., structural design determines empty aircraft weight, aerodynamic design affects required fuel weight, etc.), and thus provides a measure of merit for the HSCT as a whole. Guinta [13] suggests that minimized takeoff gross weight is also in some sense related to minimized acquisition and recurring costs for the aircraft. Figure 1 [23] illustrates a typical aircraft configuration.

The suite of optimization and analysis tools employed for this problem comprises codes developed by engineers in-house (e.g., vortex lattice subsonic aerodynamics, panel code for supersonic aerodynamics) and by third parties (e.g., optimizer, weights and structures, Harris [16] wave drag code for supersonic aerodynamics). The analysis tools are of varying complexity and computational expense, and some have coarse-grained parallel implementations. Interactions and coordination amongst programs in the suite are mostly carried out via file I/O.

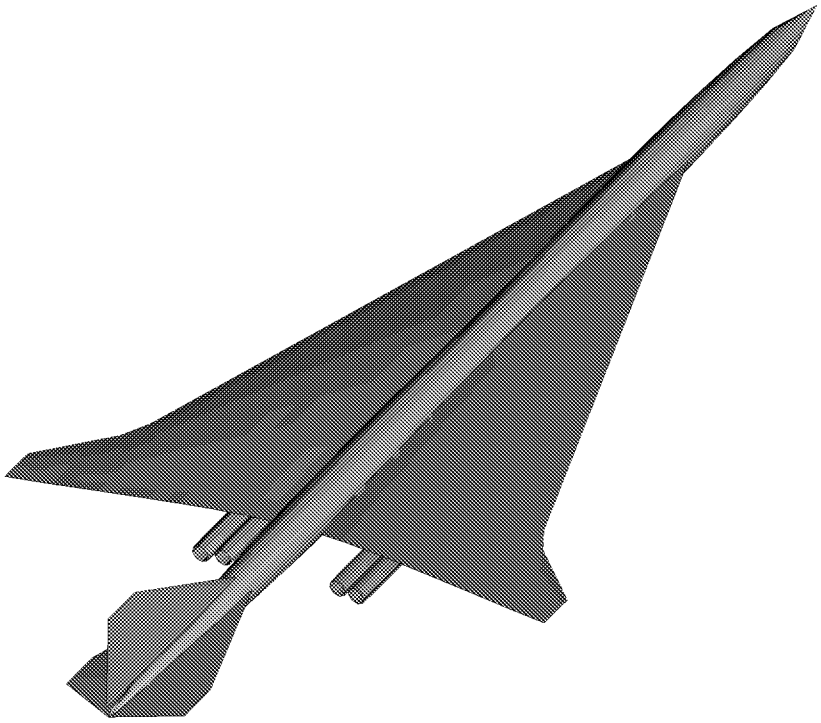

Figure 1. Typical HSCT configuration.

2.1. DESIGN VARIABLES.

Successful aircraft design optimization requires a suitable mathematical characterization of configuration parameters. Typically a configuration has $n \leq 50$ design variables. In this particular case, 29 variables are used to define the HSCT in terms of geometric—wing-body-nacelle—layout (twenty six variables) and mission profile (three variables). See Table 1 [13] for descriptions and typical values of all design variables. The wing is parametrized with eight variables for planform (see Figure 2 [13]) and five variables for leading edge and airfoil shape properties (see Figure 3 [13]). Two variables express the engine nacelle locations along the wing semi-span. The fuselage shape is defined with eight variables specifying the axial location and radius for each of four restraint points along its fixed 300 ft length. The horizontal and vertical tails are trapezoidal planforms whose areas each comprise a design variable. The thrust of the engine is also a variable. Internal volume of the aircraft is fixed at $23,270$ ft^3.

The idealized mission profile is divided into three segments—takeoff, supersonic leg at Mach 2.4, and landing. There are three variables related to the mission—flight fuel weight, climb rate, and initial supersonic cruise/climb altitude.

2.2. CONSTRAINTS.

The HSCT optimization process is subject to 69 explicit nonlinear constraints of varying complexity and computational expense. The least expensive to evaluate are geometric constraints that are used to eliminate physically senseless designs involving negative lengths, zero thickness, etc. Aerodynamic and performance constraints vary from moderately expensive (e.g., stability issues) to computationally intensive (range $\geq 5,500$). Table 2 [13] lists all constraints with short descriptions.

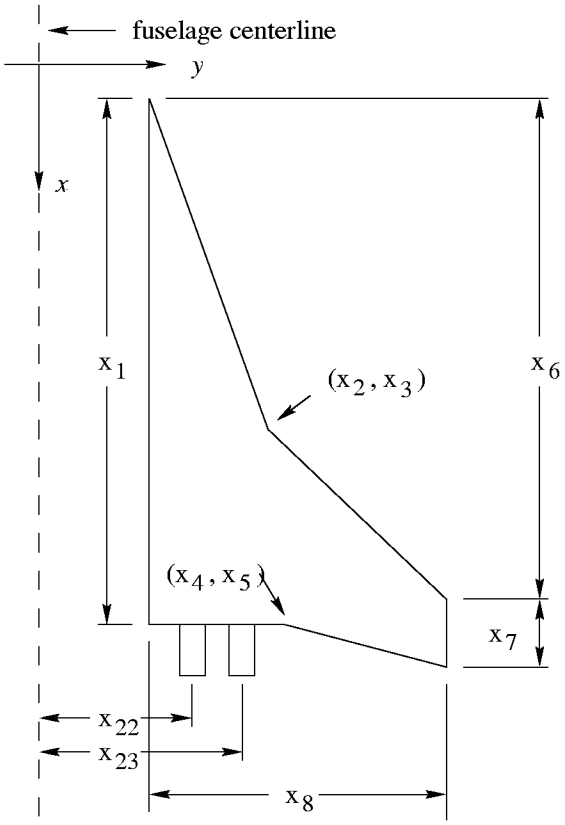

Figure 2. Wing planform design variables.

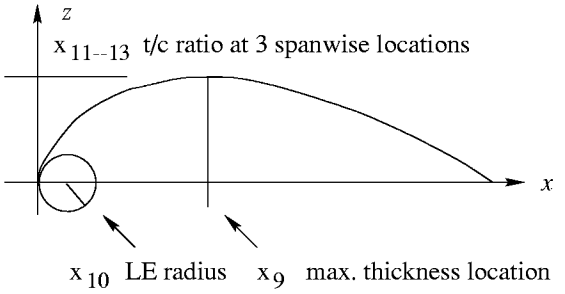

Figure 3. Wing airfoil thickness design variables.

Table 1. Design variables and typical values.

Index	Typical Value	Description
1	181.48	Wing root chord
2	155.90	LE break point, x (ft)
3	49.20	LE break point, y (ft)
4	181.60	TE break point, x (ft)
5	64.20	TE break point, y (ft)
6	169.50	LE wing tip, x (ft)
7	7.00	Wing tip chord (ft)
8	74.90	Wing semi-span (ft)
9	0.40	Chordwise location of max. thickness
10	3.69	LE radius parameter
11	2.58	Airfoil t/c ratio at root, (%)
12	2.16	Airfoil t/c ratio at LE break, (%)
13	1.80	Airfoil t/c ratio at LE tip, (%)
14	2.20	Fuselage restraint 1, x (ft)
15	1.06	Fuselage restraint 1, y (ft)
16	12.20	Fuselage restraint 2, x (ft)
17	3.50	Fuselage restraint 2, y (ft)
18	132.46	Fuselage restraint 3, x (ft)
19	5.34	Fuselage restraint 3, y (ft)
20	248.67	Fuselage restraint 4, x (ft)
21	4.67	Fuselage restraint 4, y (ft)
22	26.23	Nacelle 1 location (ft)
23	32.39	Nacelle 2 location (ft)
24	697.90	Vertical tail area (ft^2)
25	713.00	Horizontal tail area (ft^2)
26	39000.00	Thrust per engine (lb)
27	322617.00	Flight fuel (lb)
28	64794.00	Starting cruise/climb altitude (ft)
29	33.90	Supersonic cruise/climb rate (ft/min)

Table 2. Optimization constraints.

Index	Constraint
Geometric Constraints	
1	Fuel volume $\leq 50\%$ wing volume
2	Airfoil section spacing at $C_{tip} \geq 3.0$ ft
3–20	Wing chord ≥ 7.0 ft
21	LE break within wing semi-span
22	TE break within wing semi-span
23	Root chord t/c ratio $\geq 1.5\%$
24	LE break chord t/c ratio $\geq 1.5\%$
25	Tip chord t/c ratio $\geq 1.5\%$
26–30	Fuselage restraints
31	Nacelle 1 outboard of fuselage
32	Nacelle 1 inboard of nacelle 2
33	Nacelle 2 inboard of semi-span
Aerodynamic/Performance Constraints	
34	Range ≥ 5500 nautical miles
35	C_L at landing speed ≤ 1
36–53	Section C_L at landing ≤ 2
54	Landing angle of attack $\leq 12°$
55–58	Engine scrape at landing
59	Wing tip scrape at landing
60	LE break scrape at landing
61	Rudder deflection $\leq 22.5°$
62	Bank angle at landing $\leq 5°$
63	Tail deflection at approach $\leq 22.5°$
64	Takeoff rotation to occur $\leq V_{min}$
65	Engine-out limit with vertical tail
66	Balanced field length ≤ 11000 ft
67–69	Mission segments: thrust available $\geq$ thrust required

2.3. MULTI-FIDELITY ANALYSIS.

Minimizing TOGW requires a large number of disciplinary analyses (e.g., structural, aerodynamic), so that the optimal configuration(s) can be found. The computational cost of sophisticated analysis techniques becomes prohibitive as the number of design variables grows (≥ 5), and simpler methods are not accurate enough. A multi-fidelity approach employs methods of varying complexity and computational cost, so that optimization becomes feasible.

Initially, the reasonable design space paradigm employs geometric and low-fidelity analyses to constrain the design space, so that many grossly unreasonable configurations are excluded. The resulting space is called the reasonable design space. High fidelity analyses are then used to construct polynomial approximations, referred to as response surfaces, for the reasonable region. The optimizer works with response surfaces instead of the actual high fidelity analyses, because the former smooth out numerical noise and once generated are much faster and simpler to work with. Additionally, more than one response surface can be generated concurrently.

Unfortunately, the complexity and accuracy of polynomial approximations are adversely affected as the number of design variables increases (≥ 20). For this reason, low fidelity analyses are used to reduce the dimensionality and cost of polynomial models by identifying intervening variables and important terms to be used in reduced term models.

3. REASONABLE DESIGN SPACE PARADIGM.

Defining the reasonable design space consists of evaluating configurations at extreme points (vertices) in a box that contains the region of interest. At these extreme points, designs are found that often prove to be nonsensical on the basis of geometrical constraints or from estimates of the objective function and constraints based on low-fidelity analyses. These low fidelity analyses cannot accurately evaluate constraints, but they allow identification of points that are obviously meaningless. Unreasonable designs are then moved towards the center of the box, using a linear bisection algorithm, until they are no longer in gross violation of the constraints. The edge of the reasonable design space is determined in this manner.

3.1. DESIGN OF EXPERIMENTS THEORY.

A point selection algorithm is needed to generate the configurations from the box—a p-cube, centered at the origin, where p is the number of design variables—that will be used to define the reasonable design space. A full factorial design is a possible choice, but it will result in an unwieldy number of configurations. For example, a 25 variable problem with two levels for each design variable results in $2^{25} \approx 33$ million points. With an average of three evaluations needed to bring a point to the reasonable design space, this would require about 100 million low-fidelity analyses. Presently, this computation is prohibitive, and a scheme based on the partially balanced incomplete block (PBIB) design [17] is used to generate points.

A PBIB of *order* n consists of points where combinations of n, usually between two and four, variables at a time change their level. The *level* l signifies how many different discrete values a variable can assume [4]. For example, a variable allowed to take values in $\{-1, 0, 1\}$ has level three [22]. The total number of configurations generated by this scheme is

$$\sum_{i=0}^{n} l^i \binom{p}{i},$$

where n is the order, p is the number of design variables, and l is the level. In effect, this results in all combinations where 1 through n variables can each take any one of l values,

while the remaining variables are held at a nominal value. The nominal point, where all variables are at their nominal value, is also included ($i = 0$ in the above formula). For example, the number of configurations that would have to be evaluated when $l = 2$, $p = 25$, and $n = 4$ is

$$\sum_{i=0}^{4} 2^i \binom{25}{i} = 222051.$$

Clearly this is a much smaller set of points than produced with a full factorial design. Unfortunately, using a PBIB point sample reduces the coverage of the reasonable design space, and optimization often leads to unexplored corners of the design space.

4. PARALLELIZATION STRATEGY.

The basic algorithm behind the reasonable design space paradigm consists of generating a partially balanced incomplete block (PBIB) design of specific size, evaluating all configurations in the block around a nominal design using low fidelity analysis and constraints, and moving infeasible designs towards the center until they become acceptable. The method for coercing feasibility is linear bisection, where the values of the active variables are moved towards the nominal values until the boundary of the feasible region is found within a specified tolerance interval. The parallel version was implemented so that only one arbitrary manager node P_M deals with file I/O—reading initialization files, and storing results on disk. The manager node is also responsible for disseminating initialization information (e.g., nominal design variable values, PBIB size, etc.) to and gathering results from all other nodes P_i. All nodes, including P_M, generate a respective part $PBIB_i$ of the PBIB vector and perform evaluations on those configurations. The pseudocode below describes the parallel version algorithmically.

if P_M **then**
  read initialization files;
  broadcast initialization data to all P_i;
end if
receive initialization data;
generate $PBIB_i$;
for all configurations x_j in $PBIB_i$
  evaluate constraints for x_j;
  until violation within tolerance limit
    move x_j towards closest reasonable configuration using linear bisection;
    evaluate constraints for x_j;
  end until
end for
send $PBIB_i$ to P_M;

if P_M **then**

gather and **save** all $PBIB_i$;

end if

Even though each processor gets roughly the same number of configurations initially, a load imbalance is likely to occur when an indeterminate number of total evaluations are required. To achieve better balance, the algorithm was augmented to include logics for distributed dynamic load balancing and termination detection. The dynamic load balancing logic entails a processor to start searching for more work when it has under a certain threshold of configurations left to evaluate:

while (local work $\leq$ *threshold* $\wedge$ termination not detected)

search for work;

end while

Similarly, termination detection logic monitors certain conditions in order to establish that all work has been performed.

when termination condition

broadcast termination to all P_i;

end process;

4.1. PARALLEL IMPLEMENTATION.

The distributed control algorithms were implemented in C to mesh with the existing analysis codes that were in both C and FORTRAN 77.

4.1.1. MPI.

The Message Passing Interface (MPI) [31] is a message passing standard developed by the MPI forum—a group of more than 80 people representing universities, research centers, vendors and manufacturers of parallel systems. As a communications protocol MPI is platform independent, thread-safe, and has a lot of useful functionality—combining the

best features of several existing messaging protocols [31]. A brief discussion of these attributes follows.

- **Platform independence:** MPI was developed to work on parallel platforms regardless of underlying architecture. This abstraction over native communication protocols makes MPI applications portable across architectures (distributed memory, shared memory, or network clusters) as long as an MPI implementation for the desired platform exists. For many architectures MPI implementations are readily available, since the standard is widely supported by computer manufacturers.
- **Built-in functionality:** One of the important advantages of MPI is that it provides reliable communications, so the programmer does not have to deal with communication failures (see assumptions in Chapter 5.1). The standard also incorporates mechanisms for point-to-point and collective communication (e.g., broadcast, scatter, gather, etc.), overlapping computation and communication, process topologies and groups, and awareness and manipulation of the parallel environment. Much of this functionality has been incorporated in the parallel version of the code.
- **Thread-safety:** The dynamic load balancing code exploits a multi-threaded paradigm. This implies that all modules and packages used in the code have to be designed to work with threads, otherwise results are unpredictable.

4.1.2. THREADS.

The implementation of the load balanced code is multi-threaded based on the POSIX threads (pthreads) package. Threads are distinct concurrent paths of execution within the same OS process that get scheduled within the allotted time of their parent process. Different scheduling techniques can be used depending on the package and the operating system support. For more detail see [30]. One of the challenging aspects of multithreaded design is that threads share access to their parent process' memory. This calls for mutual exclusion and synchronization techniques, like semaphores, monitors, etc., that can introduce extra complexity to the code. An advantage of this approach is that it exploits concurrency at the processor level. For example, a thread could be running on the I/O controller, another

on the network service node, and a third one could be performing computations on the processing unit. Such concurrency can also be achieved by using nonblocking I/O or MPI calls, but organizing each logical task within the process in a thread can provide a finer-grained concurrency and a more intuitive design. For example, Kumar, Grama, and Rao show a state diagram describing a "generic parallel formulation" [25], where the grain of concurrency depends on the fixed unit of work. In a typical multithreaded approach threads that have no work stay idle without consuming processing cycles, and start working only when they are signaled that there is more work to be done, thus avoiding busy-wait.

In this implementation, one thread is simply a worker responsible for evaluating configurations from the local vector, and sleeping when there is no work. A second thread deals with message passing and processing (e.g., placing incoming work in the vector for the worker, signaling threads about the occurrence of certain conditions, such as termination, etc.). Global round robin logic with message combining is encapsulated as a separate thread that cycles between a sleep/delay phase and the routing of GRR-MC messages along a spanning tree topology. Mutual exclusion for shared data, like the local configurations vector, is achieved with semaphores. The use of POSIX threads introduced a lot of complexities derived not so much from using semaphores to maintain mutual exclusion and synchronization, but rather due to technical issues like thread safety of library calls, testing a distributed system with many players, etc. On the good side, design and implementation ended up being modular and relatively encapsulated.

5. DISTRIBUTED ALGORITHMS.

5.1. ASSUMPTIONS.

Let W be the total number of configurations to be evaluated, and let N be the number of processors available for computation. The following conditions are assumed for the communications network:

- communication channels are reliable, i.e., there is no message loss, corruption, duplication, or spoofing;
- communication channels do not necessarily obey the FIFO rule;
- messages take an unpredictable, but *finite* amount of time to reach their destination;
- a message that has been sent is considered in transition until it has been processed at its destination;
- each processor has knowledge of its own identity;
- the processors are completely connected, i.e., there is either a direct or an indirect communication route from every processor to every other;
- the network is fixed, i.e., its does not change size dynamically. Thus each processor has knowledge of the total number of processors in the network.

It is a prerequisite for the dynamic load balancing and termination detection paradigms described below that initially all work is distributed evenly amongst all processors. Thus, every node starts off with an initial load equal to approximately total work divided by number of processors W/N. For the remaining part of this chapter *node* and *processor* will be used interchangeably, and *task*, *work*, and *load* shall refer to the process of evaluating and possibly coercing a configuration, represented by a row of the PBIB design matrix, to a reasonable design.

5.2. DYNAMIC LOAD BALANCING.

Both algorithms described in this chapter have the following attributes.

- **Nonpreemptive:** partially executed tasks are not transferred. Preemption can be very expensive in terms of transferring a task's state.
- **Receiver initiated:** work transfer is initiated by receiving nodes. This is more suitable here, since total work is fixed, and there is no good heuristic for estimating if a node is comparatively overloaded, i.e., how long a task will take.
- **Threshold transfer policy:** a node starts looking for more work when the number of its tasks has dropped below a certain threshold.
- **Fixed ratio splitting policy:** when a node is about to transfer work, it uses a fixed ratio α to split its work W_i to send away αW_i. α is fixed because the algorithms will not be collecting any system information to help them adapt α to the global state. ($\alpha = 0.5$ for the results here.)
- **No information policy:** the nodes do not attempt to gather any information about the system state. The potential overhead inherent in information collection outweighs the benefits, since the communication network is static, processors are aware of all other processors, and no work is created dynamically. Surveys of dynamic load balancing can be found in [21], [30].

5.2.1. RANDOM POLLING (RP).

When a processor runs out of work it sends a request to a randomly selected processor. This continues until the processor finds work or there is no more work in the system and termination is established. Each processor is equally likely to be selected. This is a totally distributed algorithm, and has no bottlenecks due to centralized control. One drawback is that the communication overhead may become quite large due to the unpredictable number of random requests generated. Also, in the worst case, there is no guarantee that any of the idle processors will ever be requested for work, and effectively no load balancing may be achieved. Detailed analysis and some implementation results on random polling are treated by Sanders in [28], [29].

5.2.2. GLOBAL ROUND ROBIN WITH MESSAGE COMBINING (GRR-MC).

The idea behind a global round robin is to make sure that successive work requests go to processors in a round robin fashion. For example, in a parallel system of N processors, if the first work request goes to processor 0, the second one will go to processor 1, such that the ith request will be sent to processor $i \bmod N$. All processors will have been polled for work in N requests. This scheme requires global knowledge of which processor, say T, is to be polled next. A designated processor acts as the global round robin manager, and keeps track of T. When a node needs work it will refer to the manager for the current value of T. Before responding to other queries the manager will increment T to $T + 1 \bmod N$. The node looking for work can then send a request for tasks to the processor whose identity is equal to T. A major drawback of this scheme is that as N grows and the work requests increase, the manager will become congested with queries, posing a severe bottleneck.

Kumar, Grama, and Rao [25] suggested that message combining be introduced to reduce the contention for access to the manager. Processors are organized in a binary spanning tree with the manager as the root, where each processor is a leaf of this tree. When a processor needs the value of T it sends a request up the spanning tree towards towards the root. Each processor at an intermediate node of the tree holds requests received from its children for some predefined time d before it propagates them up in one combined request. If i is the cumulative number of requests for T received at the root from one of its children, then T is incremented by i before a request from another child is processed. The value of T before it was incremented is percolated back down the tree through the child. Information about combined requests is kept in tables at intermediate tree nodes until they are granted, so that the correct value of T percolates down the tree. An example of global round robin with message combining is illustrated in Figure 1.

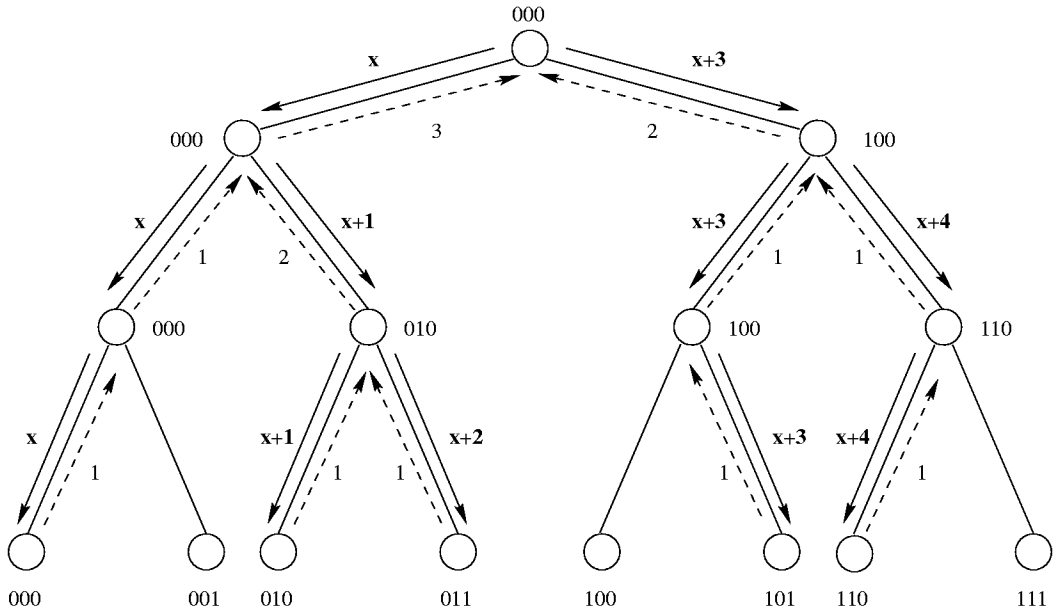

Figure 4. GRR-MC on a spanning tree, where x is the value of T, and $N = 8$.

5.3. TERMINATION DETECTION.

Termination is part of the global state of a distributed system, because it depends on the global availability of work, as opposed to the work load of a single processor. The definition of global termination for this system implies that all processors are idle, and that there are no work transfer messages in transit. In other words, since no additional work is created on the fly, global termination has occurred when all computation is complete. An idle node is one which has no work, and is searching for work using one of the dynamic load balancing algorithms described above. A busy node is one which has work to perform. A processor can change its state from busy to idle only when it finishes its tasks, and from idle to busy only when it receives a work transfer message. Clearly, termination is a stable state, because if all processes are idle, and there are no messages in transit, then no node will receive a work transfer message, and thus change its status to busy.

The global state of a distributed system can be captured in two ways, synchronously and asynchronously. The former can be achieved by freezing all processes on all processors and inspecting the state of each processor and each communication channel. This can be very time consuming when the number of processors is large, and more than one global state capture may need to be performed. Both of the algorithms described below establish termination asynchronously.

5.3.1. GLOBAL TASK COUNT (GTC).

The idea behind global task count is to keep track of all finished tasks, and use this to detect when all work has been performed, i.e., establish termination. This algorithm is applicable because the total number of tasks is available, and fixed. One processor, the manager, is responsible for keeping track of the finished tasks count C. Initially, C is set to 0. Whenever a processor completes its set of tasks, it sends a notification to the manager with the number of tasks that it completed. Upon receiving such a message the manager increments C accordingly. Eventually, as all has been performed, the value of C becomes equal to the known total number of tasks. At this point, the manager notifies all processors that termination has occurred.

Global task count detects termination immediately after it occurs, which makes it very fast. The total number of messages sent by a node to the manager is equal to the number of times that the node became busy with work, including its initial load. A potential drawback is that sending messages to a single manager may become a bottleneck, as the number of processors increases. On the other hand, total completion notifications are expected to be of order N, and to be spread out in time. This algorithm is very similar to Mattern's Credit Recovery Algorithm described in [32] and Huang's algorithm treated in [30]. Task count here corresponds to credits in Mattern's and Huang's algorithms that are not scaled to 1. The fact that credits are not scaled to 1 has the advantage of avoiding floating point representation issues that would otherwise be encountered. A separate proof of correctness for global task count is considered redundant.

5.3.2. TOKEN PASSING (TP).

Token passing is a wave algorithm for a ring topology. For a thorough discussion of wave algorithms see [33]. A wave is a pass of the token around the ring where all processors have asynchronously testified to being idle. This is not enough to claim termination, since all nodes are polled at different times, and with dynamic load balancing, it is uncertain if they remained idle or later became busy. A second wave is needed to ascertain that there has been no change in the status of any processor. For a similar algorithm, see [6]. Termination is detected in at most two waves or $2N$ messages, after it occurs. The total number of messages used depends on the total number of times the token is passed around the ring, but is bounded below by $2N$.

Each processor P_i keeps track of its state in a local flag $idle_i$. Initially, $idle_i$ is set to $false$ if a processor starts off with some load, otherwise it is set to *true*. Consequently, $idle_i$ is set to $false$ every time a processor receives more work as a result of dynamic load balancing. A token containing a counter T_c is being passed among all processors in a circular fashion. Upon receiving the token, a processor holds it until it has finished all its pending work $tasks_i$, is not expecting replies to work requests, and has made more than U unsuccessful attempts to find work. At that point, P_i checks the value of its $idle_i$ flag. In case $idle_i$ is *true* the processor increments the token counter T_c by 1. In the case where $idle_i$ is $false$, the T_c is reset to 0, and the value of $idle_i$ is set to *true*. After this, if the token counter happens to be equal to the number of processors N, termination is established and all processors are notified. Otherwise, the token is sent to the next processor in the ring. Pseudo code for this scheme for each processor P_i follows.

on start-up

token arrives at P_0 with $T_c := 0$;

if $tasks_i > 0$ **then** $idle_i := false$

else $idle_i := true$;

when *token* arrives at P_i

wait until ($tasks_i = \emptyset \wedge$ expected replies to work requests by $P_i = \emptyset \wedge$

unsuccessful consecutive work requests by $P_i \geq U$);

if $idle_i = true$ **then** $T_c := T_c + 1$

else $T_c := 0$;

$idle_i := true$;

if $T_c = N$ **then** establish termination

else send *token* to neighbor $P_{(i+1) \bmod N}$;

when extra work arrives at P_i

$idle_i := false$;

U is an algorithmic parameter, whose effect on performance is discussed in the parametric study chapter. It can be shown that $T_c = N \Rightarrow$ global termination because $T_c = N$ means that each processor P_i has consistently had no local work, for two consecutive waves around the ring, i.e., all processors are idle. Since the token is passed only when a processor expects no replies to work requests, i.e., it is passed between request-reply cycles only, it is clear that there is no work in transition. On the other hand, if global termination takes place all processors will be idle making unsuccessful attempts to find work. Eventually, for all P_i the number of unsuccessful attempts to find work will become more than U, allowing each processor to pass the token to its neighbor when it is not expecting a reply to a request for work. This ensures that for all P_i, $idle_i$ will become *true* in the first wave, and that for all P_i, T_c will be incremented during the second wave until $T_c = N$. Thus, $T_c = N \iff$ global termination.

6. PARALLEL PERFORMANCE.

Table 3. Intel Paragon parallel times (hh:mm:ss) for low fidelity analysis of 2,026,231 HSCT designs.

N	RP		GRR-MC		Static
	GTC	TP	GTC	TP	
32	8:28:38 (6:38)	8:38:23 (2:33)	8:30:00 (1:30)	8:39:41 (:48)	12:48:11 (1:52)
64	4:08:05 (:03)	4:13:08 (:04)	4:13:08 (:02)	4:18:09 (:02)	7:06:59 (:09)
128	2:11:46	2:12:54	2:14:04	2:17:36	3:43:30
256	57:39	1:03:46	59:27	1:08:24	1:54:58
512	31:16	33:04	33:34	34:26	1:01:49
1024	15:20	15:43	17:30	17:27	29:26

To test scalability and efficiency a relatively large data set with approximately 2 million (2,026,231) designs was generated using the point selection algorithm described earlier with order 4 and level 3. All runs have been performed on Intel Paragon platforms, which have a mesh architecture with Intel i860 XP processors comprising the computing entities. Figures 5–7 are snapshots produced with the *nupshot* utility, showing the states of nodes during execution for a small sample problem on $N = 7$ nodes. In these snapshots a processor can be in one of three states, performing useful computation, sitting idle, or reading initialization files—file I/O. When dynamic load balancing is not in effect (Figure 5), processors appear to spend half of their time being idle. With GRR-MC (Figure 6) and RP (Figure 7) idle states are more scattered, and seem significantly reduced. It can also be seen that even though RP and GRR-MC result in different distributions, both are very effective.

Table 3 shows execution times from the Intel Paragon computer XP/S 7 (100 compute nodes) at Virginia Tech, and the Intel Paragon XP/S 5, XP/S 35, and XP/S 150 (128, 512, 1024 compute nodes, respectively) computers at the Oak Ridge National Laboratory Center for Computational Sciences. Times are given in hours, minutes, and seconds; for $N \leq 64$ the average of five runs is reported, with the standard deviation in parentheses under the time. The same problem run on the XP/S 7 XP/S 5, and XP/S 35 Paragons takes

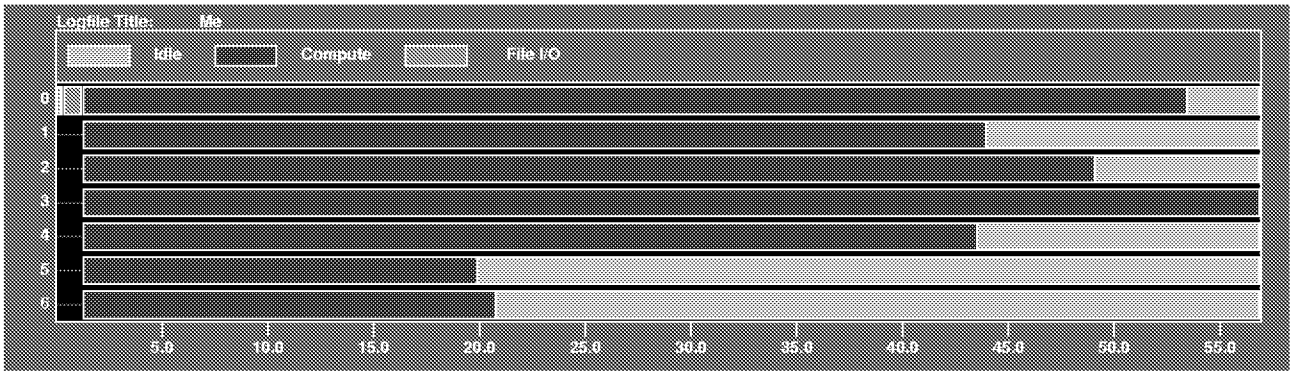

Figure 5. Snapshot from *nupshot* utility of static load distribution, $N = 7$.

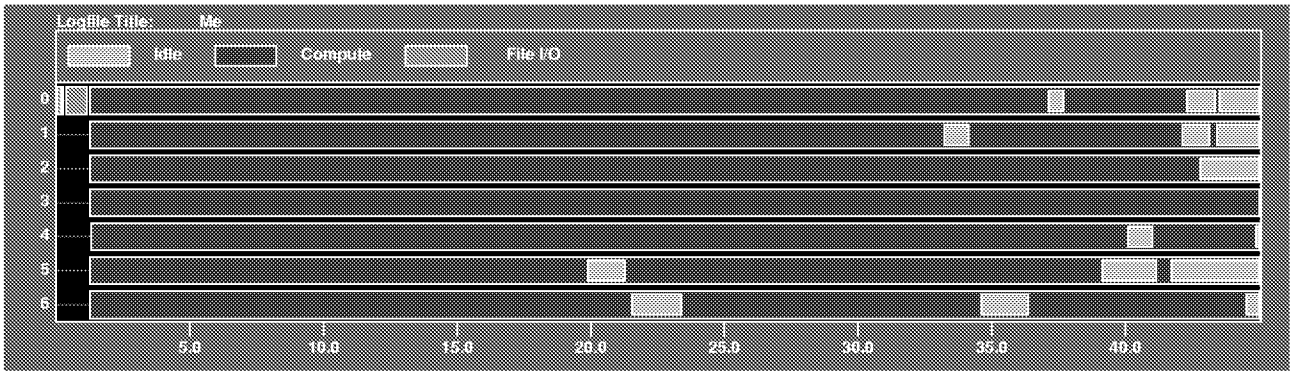

Figure 6. Snapshot from *nupshot* utility of GRR-MC with global task count termination, $N = 7$.

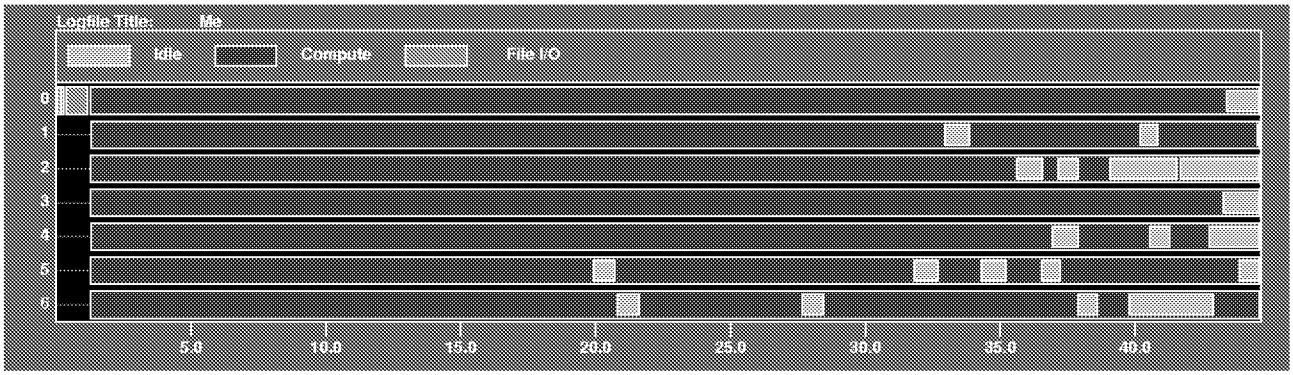

Figure 7. Snapshot from *nupshot* utility of RP with global task count termination, $N = 7$.

comparable amounts of time; times on the XP/S 150 Paragon tend to be a little higher (4 to 12 percent) than similar runs on the XP/S 35. Random polling uses the same fixed seed for all runs. For all other results, $N \geq 128$, only one run was completed because of limited access to larger machines. The table starts from $N = 32$ nodes instead of $N = 1$ because the time required to run 2 million designs on one processor is prohibitive (> 400 hours). Furthermore, the current implementation generates all the PBIB designs in one chunk, so the memory required (535 MBytes) for all designs would also be prohibitive. The original serial code has not been used for comparisons because its intensive use of file I/O makes it extremely inefficient, and thus infeasible even for problems of moderate size. Times in Table 3 do not include disk storage (1.2GBytes) for the final results. Figures 8 and 9 show speedup for all schemes, based on the execution times for $N = 32$ processors.

Several observations can be made from Figures 8–9 and Table 3.

(1) **Scalability:** all algorithms, including static distribution, scale well for $N \leq 1024$ nodes, with random polling showing no noticeable degradation in efficiency at $N = 1024$ nodes.

(2) **Dynamic vs. static:** both dynamic load balancing techniques seem to be very effective, 35 to 50 percent better than static distribution, and this difference increases with the number of processors N.

(3) **Stable execution times:** the standard deviations of total execution time for runs on 32 and 64 processors are very small, which indicates that performance is relatively stable. Random polling is expected to have more variance in execution time when the seed is not fixed, but not a significant difference.

(4) **Superlinear speedup:** the latter rows of Table 3 exhibit superlinear speedup for global round robin with message combining and random polling. This implies that at 32 nodes the memory requirement (18 MBytes) for working with a relatively large number of tasks ($\approx 63,319$) per node can degrade performance on the XPS/7 platform due to resource starvation. See Quinn [26] for a discussion of general circumstances for superlinear speedup.

(5) **Global task count vs. token passing:** Global task count seems to outperform token passing for $N \leq 1024$ with GRR-MC and RP, but the relative difference decreases for

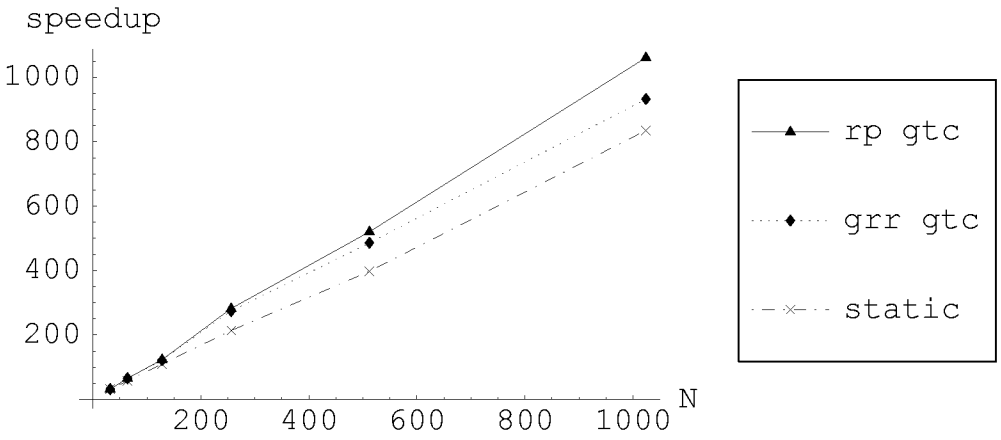

Figure 8. Speedep with base $N = 32$ for RP and GRR-MC with global task count, on $N = 2^{\{5...10\}}$ processors.

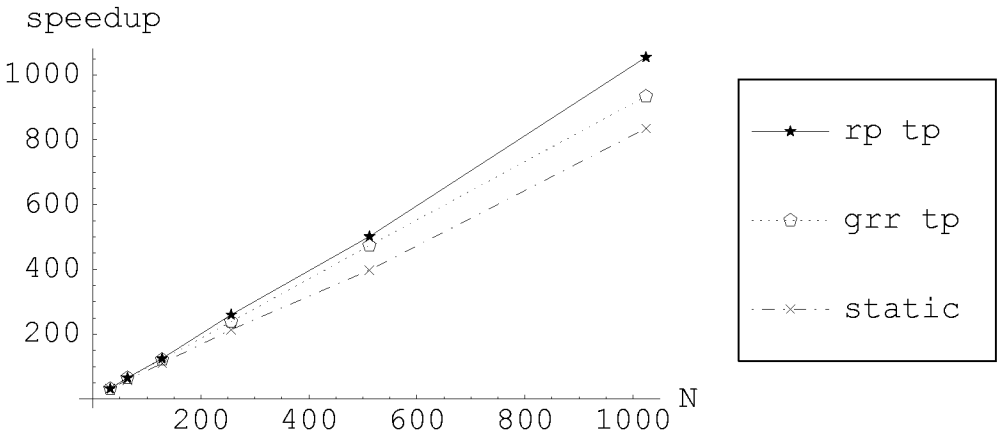

Figure 9. Speedep with base $N = 32$ for RP and GRR-MC with token passing, on $N = 2^{\{5...10\}}$ processors.

larger N. Clearly, the overhead involved in processing all completion messages ($\geq N$) by one manager node under global task count increases with N.

(6) **Random polling vs. global round robin with message combining:** With both termination detection schemes random polling clearly outperforms global round robin with message combining. The relative difference in execution times increases as N becomes larger. The simplicity of the random polling algorithm leads to the lack of any significant overhead. Contention conditions are unlikely to occur because messages are randomly directed and typically the number of unsuccessful work acquisition messages increases significantly only just before termination. Global round robin with message combining, on the other hand, involves a longer wait, comprised of a fair number of communication messages across the spanning tree, before it can send a work acquisition request and the price of unsuccessful work acquisition requests is higher, because they imply more time spent idle. Furthermore, on average the total number of messages processed by a node running GRR-MC is higher that that for a node running RP, since each request is propagated back and forth through as many as $\log_2 N$ other nodes. Finally, for both algorithms, the fact that all nodes start off with some load, which is expected to be relatively balanced among them for a large number of randomly long tasks, serves to decrease the initial number of unsuccessful work acquisition requests, which in turn improves performance.

7. PARAMETRIC STUDY.

The purpose of this study is to evaluate the effect, if any, of algorithmic parameters on the performance of the distributed schemes. Two dynamic load balancing parameters, splitting ratio and transfer threshold, discussed in Chapter 5.2, are reviewed, together with two algorithm-specific parameters, delay d for GRR-MC and unsuccessful work acquisition attempts threshold U for token passing (TP). Delay is defined as CPU clock ticks, where the actual wait time is the delay clock ticks multiplied by the clock resolution. See Table 4 for the sets of values used to test these parameters. The variation of random polling times for five different seeds is also examined.

Table 4. Values for algorithmic parameters.

Parameter	**Set of Values**
splitting ratio α	$\{0.10, 0.25, 0.40, 0.50, 0.60, 0.75, 0.90\}$
transfer threshold	$\{0, 15, 30, 45, 60, 75, 90, 105\}$
unsuccessful work acquisition attempts U for TP	$\{0, 5, 10, 15, 20, 25\}$
delay d for GRR-MC in clock ticks	$\{500, 1000, 1500, 2000, 2500, 3000, 3500\}$

Comprehensive runs were initially performed with a relatively small data set of $30,915$ configurations on $N = 32$ and 64 processors. A larger number of processors N was not used because of time constraints on the larger Paragons. The trends observed were confirmed with a few runs on the large data set with $N = 64$ nodes. Both the delay d for global round robin with message combining and the random seed for random polling introduced very small fluctuations in execution times—the variation was less than 1 percent in most cases.

Variation of the unsuccessful acquisition attempts U for token passing and the transfer threshold also resulted in a very insignificant difference in execution time, and no particular pattern was observed. For instance, Figures 10 and 11 are surface plots showing how performance varies with different values for transfer threshold. The vertical axis denotes execution time in *hours*; the axis labeled *transfer threshold* is for the values $\{0, 15, 30, 45, 60, 75, 90, 105\}$ taken by this parameter; the *schemes* axis parameterizes the

schemes RP GTC, RP TP, GRR-MC GTC, GRR-MC TP for which execution time is measured. Figures 12 and 13 are similar surface plots illustrating the effect of the splitting ratio $\alpha \in \{0.10, 0.25, 0.40, 0.50, 0.60, 0.75, 0.90\}$ parameter. A difference in time occurs at the two extreme values $\alpha \in \{0.10, 0.9\}$, and even here the increase in time is at most 15 percent. Runs on 64 nodes with the large data set of 2,026,231 configurations confirm the trend at the extreme values, but also show that the increase in time becomes less than 1 percent (see Figures 14 and 15).

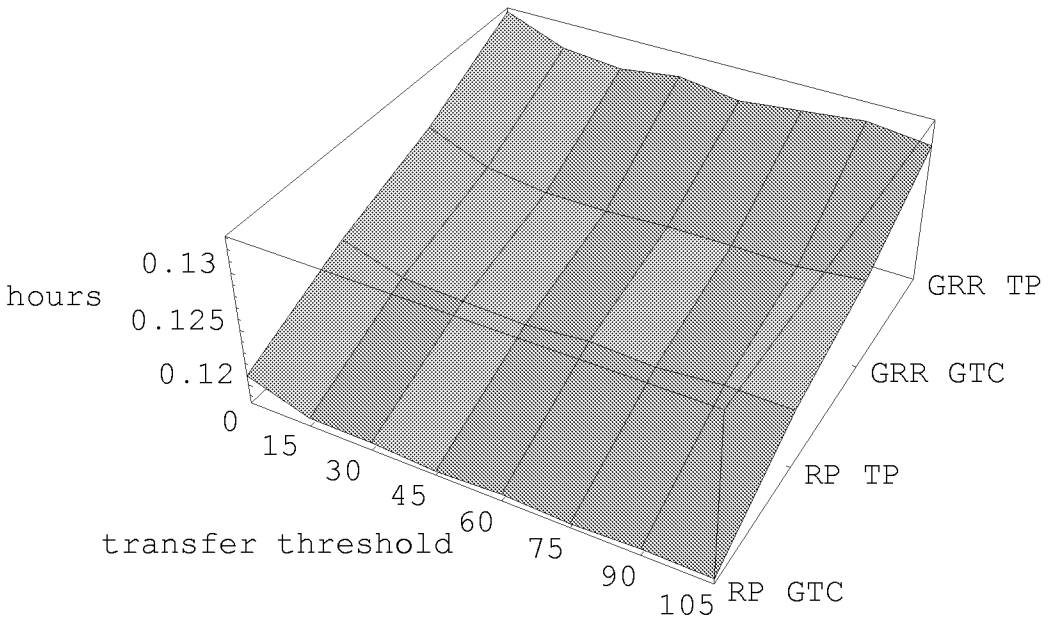

Figure 10. Effect of transfer threshold for $N = 32$ on $30,915$ designs.

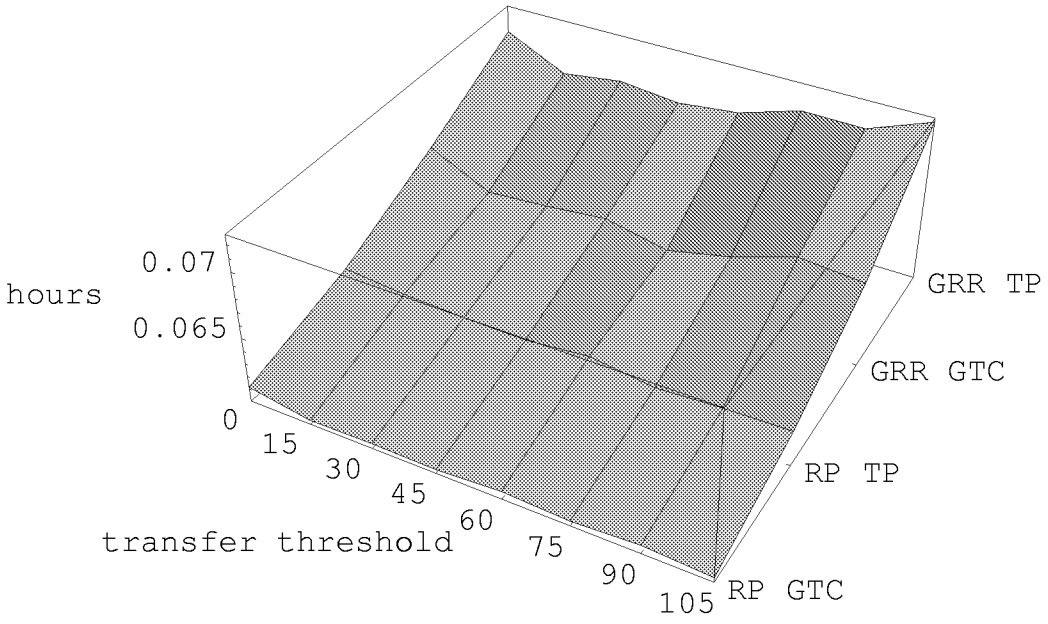

Figure 11. Effect of transfer threshold for $N = 64$ on $30,915$ designs.

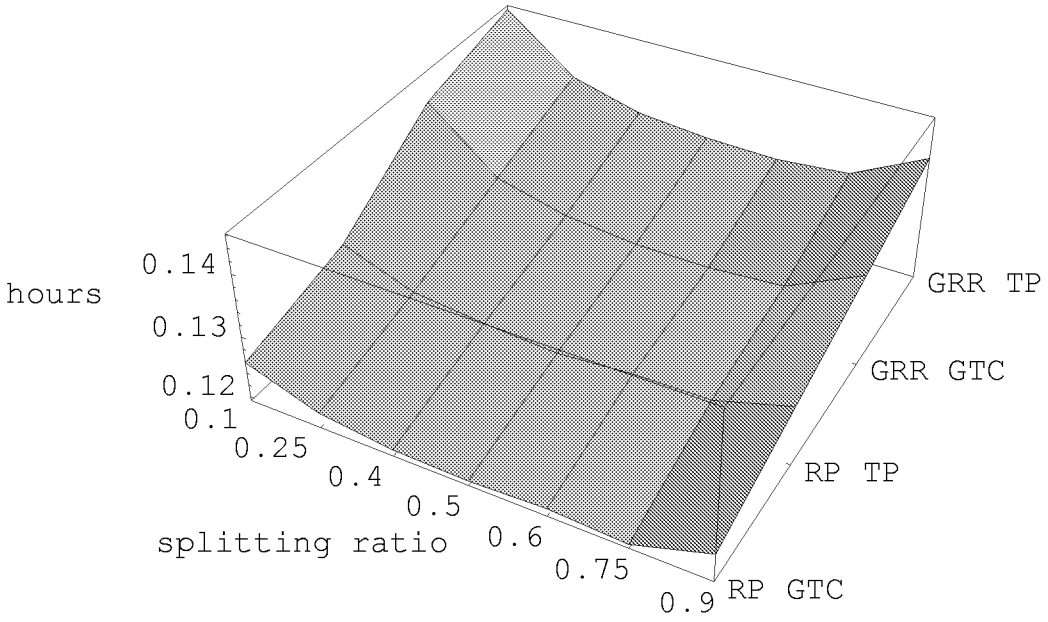

Figure 12. Effect of splitting ratio α for $N = 32$ on $30,915$ designs.

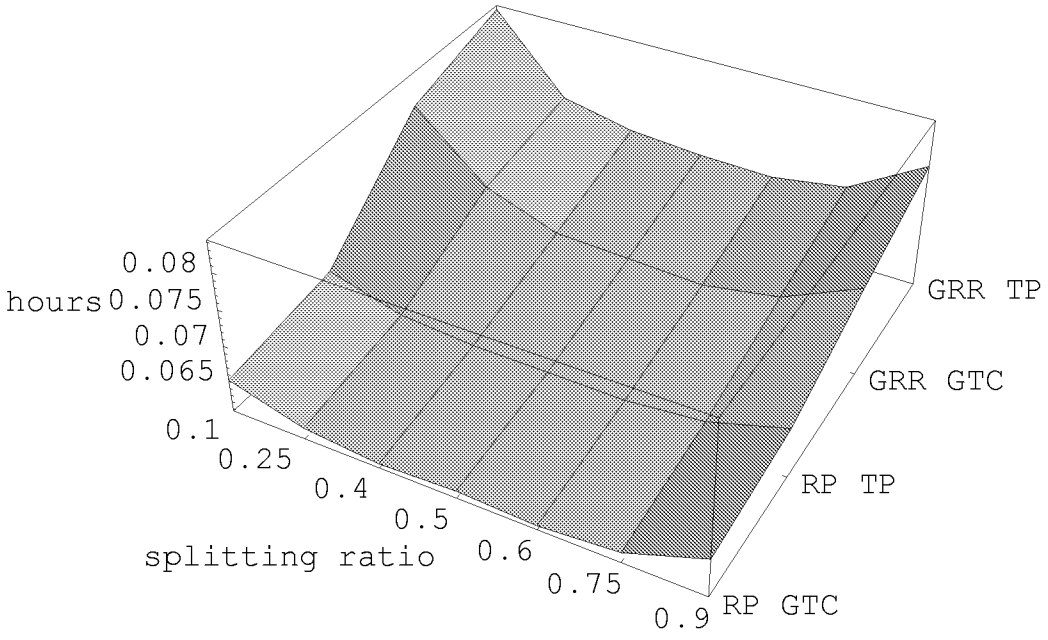

Figure 13. Effect of splitting ratio α for $N = 64$ on $30,915$ designs.

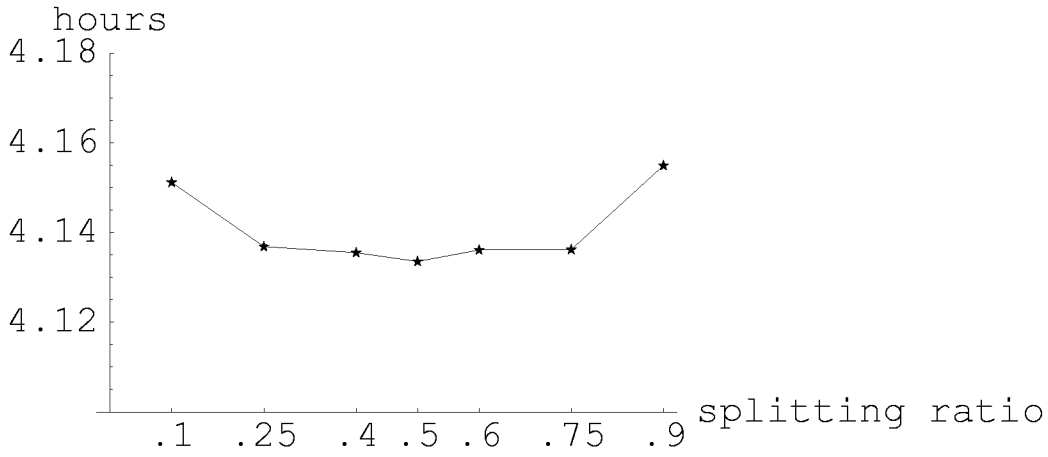

Figure 14. Effect of splitting ratio on RP GTC for $N = 64$ on $2,026,23$ designs.

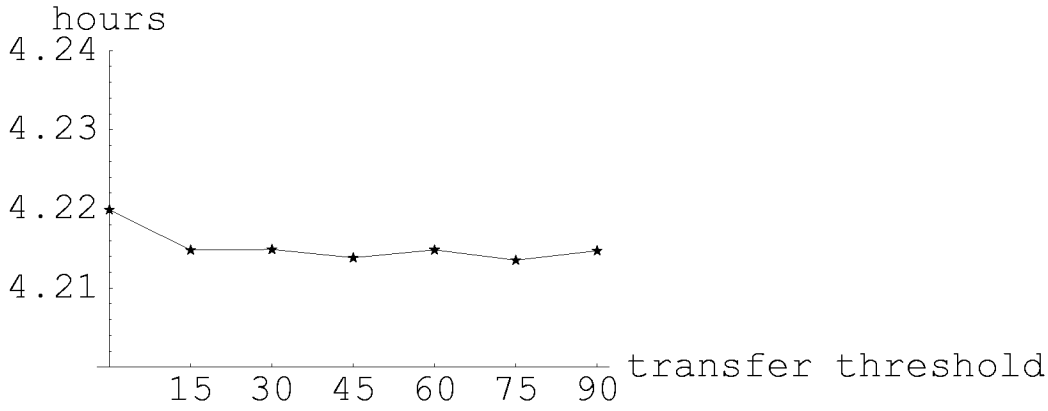

Figure 15. Effect of transfer threshold on RP TP for $N = 64$ on $2,026,23$ designs.

8. CONCLUSIONS AND FUTURE WORK.

Distributed control and load balancing techniques were applied to an aspect of the multidisciplinary design optimization of a high speed civil transport. Two dynamic load balancing algorithms (random polling and global round robin with message combining) together with two necessary termination detection schemes (global task count and token passing) were implemented for the reasonable design space identification paradigm. Performance was evaluated on up to 1024 processors for all combinations of dynamic load balancing and termination detection schemes, plus the static distribution case. The effect of various algorithmic parameters was also explored, and found to be negligible except at extreme values. The results were very encouraging in terms of the effectiveness of dynamic load balancing (35–50 percent improvement over a static distribution), and the scalability of the algorithms (speedup was essentially linear). Most importantly, the time spent identifying the reasonable design space has been dramatically decreased, permitting the low fidelity analysis of 2 million designs, which was impractical before. The logical next step is to go beyond merely identifying the reasonable design space, and to identify good design regions within the reasonable design space, which would then be passed off to mildly parallel machines (e.g., IBM SP/2 or SGI Origin 2000) for "local" high fidelity optimization.

This effort is a stepping stone towards the goal of a MDO problem solving environment that will provide a complete and convenient computing environment for interactive multidisciplinary aircraft design. As shown by the experience of Burgee et al. [7], Guruswamy [14], and many others, some crucial disciplinary analysis codes (for structural mechanics, fluid dynamics, aerodynamic analysis, propulsion, to name a few) perform very poorly in a multidisciplinary parallel computing environment. These codes represent hundreds of man-years of experience and development, and are unlikely to be rewritten for parallel machines any time soon. Thus the challenge is to find approaches to MDO (e.g., variable complexity modeling and response surface techniques) which permit the use of massively parallel computing for some phases of the process (one such phase was demonstrated here) and legacy disciplinary codes on serial computers for other phases. One highly touted solution is "network computing", but that still remains far from practical for serious large-scale multidisciplinary design.

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Appendix A: CODE FOR MESSAGE PROCESSING THREAD.

The **C** code where all threads are invoked and message handling takes place, as mentioned in Chapter 4.1.2., is listed in this appendix.

```
#include <stdio.h>
#include <stdlib.h>
#include <pthread.h>
#include <mpi.h>
#include "prof.h"       /** profiling constants **/
#include  "defines.h"    /** const definitions for structs.h **/
#include  "structs.h"    /** aircraft struct definition **/
#include  "HSCTSearch.h"
#include  "lib.h"       /** matrix functions  **/
#include "prelim.h"
#include "compute.h"
#include "grr_mc.h"
#include "random.h"
#include "worker.h"
#include "safemem.h"
#define COMM_BUFS   10
/**
Token Passing variables that are shared between the worker thread,
the token passing routine, and the message handling routine
**/
int idle, token_count_buf, token_received, unsucc_work_attempts, expecting_reply;
/*****************************************************************************
ComputationPhase:   Routine for message processing; it starts off the other
                threads respective of the algorithm parameters passed by the user.
                The main part of this routine consists of a loop that checks for
                messages and processes them.
*****************************************************************************/
int ComputationPhase(   struct cntrl_struct *cntrl, MatrixClass *dvar,
                    MatrixClass *local_points, Aircraft *aircraft,
                    Prog_Args_Struct *prog_args_struct)
{
   register int i;
   int my_rank, group_size, done_count, carryover, error_status,
      j, num_leaves, num_leaves_rcvd, child_leaves, child,
      index, target_node, test_flag, tot_sent_work,
      tot_work_rcvd, tot_work_rcvd_buf, total_msgs,
      tot_sent_work_buf[COMM_BUFS],
      *grr_msg_buf = NULL, *done_indices = NULL;
   double dbl_work_sent,
         *work_sent_buf[COMM_BUFS],
```

```
        *work_rcvd_buf = NULL, *work_sent = NULL;
Q_Element *q_el = NULL;
MPI_Request rqst_work_rqst= MPI_REQUEST_NULL,
          rqst_work_sent[COMM_BUFS], rqst_qty_work_sent[COMM_BUFS],
          *mpi_rqst = NULL;
MPI_Status  work_sent_status, work_rqst_status, terminate_status,
          carryover_status, *mpi_status = NULL;
Worker_Args_Struct worker_args;
GRR_MC_Args_Struct grr_mc_args;
MPI_Datatype MPI_MATRIX_ROW;
pthread_t   thread_id[TOTAL_THREADS];
/** Global task count termination variables **/
int buf_tasks_cmplt = 0, tasks_cmplt_count = 0 ;
/** GRR - MC variables **/
int  **msg = NULL, *data = NULL;
MPI_Comm_size( MPI_COMM_WORLD, &group_size);
MPI_Comm_rank( MPI_COMM_WORLD, &my_rank);
error_status = PRELIM_SUCCESS;
MPI_Type_contiguous( local_points->nDim+1, MPI_DOUBLE, &MPI_MATRIX_ROW);
MPI_Type_commit( &MPI_MATRIX_ROW );
/** initialization of global shared variables **/
pthread_mutex_init(&mutex_matrix, pthread_mutexattr_default);
pthread_cond_init(&cond_worker_wait, pthread_condattr_default);
tasks_matrix.nDim = local_points->nDim;
tasks_matrix.mDim = local_points->mDim;
tasks_matrix.d = local_points->d;
matrix_cur_pos = 1;
matrix_top_pos = local_points->mDim;
dlb = FALSE;
termination = FALSE;
total_msgs = TOT_MAIN_MSG_TYPES;
/** TOKEN TERMINATION   **/
if (prog_args_struct->TERM == TERM_TOKEN)
{
   expecting_reply = FALSE;
   unsucc_work_attempts = 0;
   if ((matrix_top_pos-matrix_cur_pos)+1 > 0)
      idle = FALSE;
   else
      idle = TRUE;
   token_count_buf = 0;
   if ( my_rank == MASTER_RANK)
      token_received = TRUE;
   else
      token_received = FALSE;
}
```

```
/** GRR-MC **/
if (prog_args_struct->D_L_B == D_L_B_GRR_MC)
{
   total_msgs += GetGRRMessageCount(my_rank, group_size);
   msg = MsgIntBufferCreate(my_rank,
      total_msgs-TOT_MAIN_MSG_TYPES, GRR_MC_MSG_SIZE);
   grr_msg_buf = safe_malloc(GRR_MC_MSG_SIZE*sizeof(int));
   if ( grr_msg_buf == NULL)
   {
      fprintf(stderr, "worker(%d): cannot allocate grr_msg_buf!\n",my_rank);
      return PRELIM_ERROR;
   }
}
/** RANDOM_POLLING **/
else if (prog_args_struct->D_L_B == D_L_B_RANDOM_POLLING)
{
   Init_Random_Polling(group_size,
      (unsigned int) prog_args_struct->RANDOM_SEED *my_rank);
}
/** allocation of MPI request handles for the persistent recieves **/
mpi_rqst = (MPI_Request *) safe_calloc( total_msgs, sizeof(MPI_Request));
if ( mpi_rqst == NULL )
{
   fprintf(stderr, "ComputationPhase(%d): cannot allocate mpi_rqst!\n",
          my_rank);
   return PRELIM_ERROR;
}
/** allocation of MPI structures for storing the status of persistent
   receive  requests **/
mpi_status = (MPI_Status *) safe_calloc( total_msgs, sizeof(MPI_Status));
if ( mpi_status == NULL )
{
   fprintf(stderr, "ComputationPhase(%d): cannot allocate mpi_status!\n", my_rank);
   return PRELIM_ERROR;
}
done_indices= (int *) safe_calloc( total_msgs, sizeof(int));
if ( done_indices == NULL )
{
   fprintf(stderr, "ComputationPhase(%d): cannot allocate done_indices!\n", my_rank);
   return PRELIM_ERROR;
}
/** reset MPI request handles to NULL **/
for ( i = 0; i < total_msgs; i++ )
   mpi_rqst[i] = MPI_REQUEST_NULL;
for ( i = 0; i < COMM_BUFS; i++ )
{
```

```
    rqst_work_sent[i] = MPI_REQUEST_NULL;
    work_sent_buf[i] = NULL;
    rqst_qty_work_sent[i] = MPI_REQUEST_NULL;
}
/** creation of GRR-MC thread **/
if (prog_args_struct->D_L_B == D_L_B_GRR_MC)
{
    /** create GRR-MC threads **/
    grr_mc_args.grr_mc_delay = prog_args_struct->grr_mc_delay;
    pthread_create(&thread_id[DLB_THREAD], pthread_attr_default,
        (void *)GRR_MC_Routine, (void *)&grr_mc_args);
    pthread_yield();
    pthread_yield();
}
/** creation of worker thread **/
worker_args.cntrl = (struct cntrl_struct *) cntrl;
worker_args.dvar = (MatrixClass *) dvar;
worker_args.aircraft = (Aircraft *) aircraft;
worker_args.prog_args_struct = (Prog_Args_Struct *)prog_args_struct;
pthread_create(&thread_id[WORKER_THREAD], pthread_attr_default,
    (void *)WorkerRoutine, (void *)&worker_args);
pthread_yield();
/** dynamic load balancing: initialization of a MPI persistent receive request
    for every type of message that can be received and handled
    in the processing loop.  **/
if (prog_args_struct->D_L_B != D_L_B_NONE)
{
    MPI_Recv_init( NULL, 0, MPI_INT, MPI_ANY_SOURCE,
        TAG_WORK_RQST, MPI_COMM_WORLD, &mpi_rqst[MSG_WORK_RQST] );
    MPI_Recv_init( &num_leaves_rcvd, 1, MPI_INT, MPI_ANY_SOURCE,
        TAG_TERM, MPI_COMM_WORLD, &mpi_rqst[MSG_TERM] );
    /** TOKEN TERMINATION   **/
    if (prog_args_struct->TERM == TERM_TOKEN)
    {
        MPI_Recv_init( &token_count_buf, 1, MPI_INT, MPI_ANY_SOURCE,
            TAG_TERM_TOKEN, MPI_COMM_WORLD, &mpi_rqst[MSG_TOKEN]);
    }
    /** GLOBAL TASK COUNT TERMINATION **/
    if (prog_args_struct->TERM == TERM_TASK_COUNT)
    {
        MPI_Recv_init( &buf_tasks_cmplt, 1, MPI_INT, MPI_ANY_SOURCE,
            TAG_TERM_TASKS_CMPLT, MPI_COMM_WORLD, &mpi_rqst[MSG_TERM_TASKS_CMPLT] );
    }
    MPI_Recv_init(&tot_work_rcvd_buf, 1, MPI_INT, MPI_ANY_SOURCE,
        TAG_WORK_RQST_REPLY, MPI_COMM_WORLD, &mpi_rqst[MSG_WORK_RQST_REPLY] );
    /** TOT_MAIN_MSG_TYPES-1: recive work is not initialized here **/
```

```
    MPI_Startall(TOT_MAIN_MSG_TYPES-1, mpi_rqst);
    if (prog_args_struct->D_L_B == D_L_B_GRR_MC)
    {
        /** start perisitent MPI message receive requests for all nodes that GRR-MC
            messages will be received from **/
        InitGRRRecvs(my_rank, group_size, mpi_rqst, msg, TOT_MAIN_MSG_TYPES, total_msgs);
    }
}
/** message processing loop **/
carryover= FALSE;
while(termination == FALSE && prog_args_struct->D_L_B != D_L_B_NONE)
{
    pthread_yield();
    /** test if some messages of different types have been received
       Note: MPI_Waitsome would have been more appropriate here if it was implemented without
      busy wait.  In this version of MPI, using MPI_Waitsome actually increases execution time
       roughly by a factor of 2, because of busy wait. **/
    MPI_Testsome(total_msgs, mpi_rqst, &done_count, done_indices, mpi_status);
    pthread_yield();
    pthread_yield();
    if (done_count == MPI_UNDEFINED)
    {
        if (carryover == FALSE)
            continue;
        else
            done_count=0;
    }
    if (carryover != FALSE)
    {
        done_indices[done_count] = MSG_WORK_RQST;
        memcpy(&mpi_status[done_count], &carryover_status,
            sizeof(MPI_Status));
        done_count++;
    }
    /** process all received messages **/
    for ( i = 0; (i< done_count) && (termination == FALSE); i++)
    {
        pthread_yield();
        switch (mpi_status[i].MPI_TAG)
        {
            case TAG_TERM:  /** Termination message **/
                Handle_Term_Msg(my_rank, group_size,
                    prog_args_struct->TERM, num_leaves_rcvd);
            break;
            case TAG_GRR_MC_TARGET: /** message with GRR-MC target **/
                if (msg[done_indices[i]-TOT_MAIN_MSG_TYPES][0] ==
```

```
            my_rank && (group_size > 1))
        {
            j =SendToParent( 1, my_rank, 0, 1, (int**)&grr_msg_buf,
                &rqst_work_rqst);
        }
        else
        {
            if (prog_args_struct->TERM == TERM_TOKEN)
            {
                pthread_mutex_lock(&mutex_matrix);
                    expecting_reply = TRUE;
                pthread_mutex_unlock(&mutex_matrix);
            }
            /** send work request to target node **/
            MPI_Test(&rqst_work_rqst, &test_flag, &work_rqst_status);
            MPI_Isend(NULL, 0, MPI_INT,
                msg[done_indices[i]-TOT_MAIN_MSG_TYPES][0],
                TAG_WORK_RQST, MPI_COMM_WORLD, &rqst_work_rqst);
        }
        MPI_Start(&mpi_rqst[MSG_GRR_MC_TARGET]);
    break;
    case TAG_GRR_MC_TARGET_RQST: /** GRR-MC message up the tree **/
        j = SaveMsgFromRight(my_rank,
                msg[done_indices[i]-TOT_MAIN_MSG_TYPES][0],
                msg[done_indices[i]-TOT_MAIN_MSG_TYPES][1]);
        MPI_Start(&mpi_rqst[done_indices[i]]);
    break;
    case TAG_GRR_MC_TARGET_REPLY: /** GRR-MC message down the tree */
        SaveMsgFromParent(my_rank,
                msg[done_indices[i]-TOT_MAIN_MSG_TYPES][0],
                msg[done_indices[i]-TOT_MAIN_MSG_TYPES][1]);
        MPI_Start(&mpi_rqst[done_indices[i]]);
    break;
    case TAG_WORK_RQST: /** request for work from another node **/
        j = Handle_Work_Rqst_Msg(my_rank, group_size,
                (double)prog_args_struct->D_L_B_SPLIT_RATIO,
                mpi_status[i].MPI_SOURCE, COMM_BUFS,
                rqst_qty_work_sent, tot_sent_work_buf,
                rqst_work_sent, work_sent_buf);
        switch (j)
        {
            case PRELIM_ERROR:
                error_status = PRELIM_ERROR;
            break;
            case PRELIM_SUCCESS:
                if (carryover != FALSE)
```

```
            {
                carryover == FALSE;
            }
            MPI_Start(&mpi_rqst[MSG_WORK_RQST]);
        break;
        case PRELIM_INCOMPLETE:
            if (carryover == FALSE)
            {
                memcpy( &carryover_status, &mpi_status[i],
                    sizeof(MPI_Status));
                carryover == TRUE;
            }
        break;
    }
break;
case TAG_TERM_TOKEN: /** termination token **/
    pthread_yield();
    token_received = TRUE;
    pthread_mutex_lock(&mutex_matrix);
        TokenRoutine(my_rank, group_size,
            prog_args_struct->NO_WORK_THRESHOLD);
    pthread_mutex_unlock(&mutex_matrix);
    MPI_Start(&mpi_rqst[MSG_TOKEN]);
break;
case TAG_TERM_TASKS_CMPLT: /** tasks complete message **/
    pthread_yield();
    tasks_cmplt_count += buf_tasks_cmplt;
    if ( tasks_cmplt_count ==
        (cntrl->phase_two_end-cntrl->phase_two_start)+1 )
    {
        num_leaves = group_size-1;
        MPI_Send(&num_leaves, 1, MPI_INT, my_rank, TAG_TERM,
        MPI_COMM_WORLD);
    }
    else
    {
        MPI_Start(&mpi_rqst[MSG_TERM_TASKS_CMPLT]);
    }
break;
case TAG_WORK_RQST_REPLY: /** reply to work acquisition request **/
    pthread_yield();
    if ( tot_work_rcvd_buf == 0 )
    {
        pthread_yield();
        /** TOKEN TERMINATION **/
        if (prog_args_struct->TERM == TERM_TOKEN)
```

```
    {
        unsucc_work_attempts++;
        pthread_mutex_lock(&mutex_matrix);
            expecting_reply = FALSE;
           TokenRoutine(my_rank, group_size, prog_args_struct->NO_WORK_THRESHOLD);
        pthread_mutex_unlock(&mutex_matrix);
    }
    if (prog_args_struct->D_L_B == D_L_B_RANDOM_POLLING)
    {
        /** RANDOM POLLING **/
        target_node = Generate_Random_Node(my_rank, group_size);
        /** send work request to target node **/
        /** TOKEN TERMINATION **/
        if (prog_args_struct->TERM == TERM_TOKEN)
        {
            pthread_mutex_lock(&mutex_matrix);
                expecting_reply = TRUE;
            pthread_mutex_unlock(&mutex_matrix);
        }
        MPI_Test(&rqst_work_rqst, &test_flag, &work_rqst_status);
        MPI_Isend(NULL, 0, MPI_INT, target_node, TAG_WORK_RQST,
            MPI_COMM_WORLD, &rqst_work_rqst);
    }
    else if (prog_args_struct->D_L_B
        == D_L_B_GRR_MC)
    {
        SendToParent( 1, my_rank, 0, 1, (int**)&grr_msg_buf,
                &rqst_work_rqst);
    }
}
else
{
    pthread_yield();
    if (work_rcvd_buf != NULL)
        safe_free(work_rcvd_buf);
    work_rcvd_buf = (double *)
        safe_calloc(tot_work_rcvd_buf * (tasks_matrix.nDim+1),
            sizeof(double));
    if ( work_rcvd_buf == NULL )
    {
     fprintf(stderr, "ComputationPhase(%d): cannot allocate work_rcvd_buf!\n",
            my_rank);
        error_status = PRELIM_ERROR;
    }
    MPI_Irecv( work_rcvd_buf, tot_work_rcvd_buf,
        MPI_MATRIX_ROW, mpi_status[i].MPI_SOURCE,
```

```
                    TAG_WORK, MPI_COMM_WORLD, &mpi_rqst[MSG_WORK]);
                }
                MPI_Start(&mpi_rqst[MSG_WORK_RQST_REPLY]);
            break;
            case TAG_WORK:  /** message with extra work **/
                MPI_Get_count( &mpi_status[i], MPI_MATRIX_ROW,
                    &tot_work_rcvd);
                pthread_mutex_lock(&mutex_matrix);
                    if ( AcceptWork(tot_work_rcvd, work_rcvd_buf,
                        &matrix_top_pos, &tasks_matrix) == PRELIM_ERROR )
                    {
                        error_status = PRELIM_ERROR;
                    }
                    safe_free(work_rcvd_buf);
                    work_rcvd_buf = NULL;
                    if (prog_args_struct->TERM == TERM_TOKEN)
                    {
                        unsucc_work_attempts = 0;
                        idle = FALSE;
                        expecting_reply = FALSE;
                    }
                    dlb = FALSE;
                    pthread_cond_signal(&cond_worker_wait);
                pthread_mutex_unlock(&mutex_matrix);
                pthread_yield();
            break;
            default:
                fprintf(stderr, "ComputationPhase(%d): udefined tag %d\n",
                    my_rank, mpi_status[i].MPI_TAG);
        } /** switch **/
    } /** for **/
} /** while **/
/** wait for all threads to be done **/
pthread_yield();
pthread_join(thread_id[WORKER_THREAD], NULL);
if (prog_args_struct->D_L_B == D_L_B_GRR_MC)
    pthread_join(thread_id[DLB_THREAD], NULL);
local_points->mDim = tasks_matrix.mDim;
local_points->d = tasks_matrix.d;
/** cancel pending MPI message receive requests **/
for (j = 0; j < total_msgs; j++)
{
    MPI_Test(&mpi_rqst[j], &test_flag, &mpi_status[j]);
    if ( test_flag == FALSE )
    {
        /** MPI_Cancel is not implemented for recieves in this implementation of MPI.
```

```
            Please uncomment when that changes. **/
          /*MPI_Cancel(&mpi_rqst[j] );
          MPI_Request_free(&mpi_rqst[j] )*/;
      }
  }
  /** cancel pending MPI message send requests **/
  for (i = 0; i< COMM_BUFS; i++)
  {
      MPI_Test(&rqst_work_sent[i], &test_flag, &work_sent_status);
      if ( test_flag == FALSE )
      {
          /** MPI_Cancel is just a noop for sends in this implementation of MPI. **/
          /*MPI_Cancel(&rqst_work_sent[i] );
          MPI_Request_free(&rqst_work_sent[i] );*/
      }
      MPI_Test(&rqst_qty_work_sent[i], &test_flag, &work_sent_status);
      if ( test_flag == FALSE )
      {
       /* MPI_Cancel(&rqst_qty_work_sent[i]);
          MPI_Request_free(&rqst_qty_work_sent[i]); */
      }
      if (work_sent_buf[i] != NULL)
          safe_free(work_sent_buf[i]);
  }
  MPI_Test(&rqst_work_rqst, &test_flag, &work_rqst_status);
  if ( test_flag == FALSE )
  {
      /*MPI_Cancel(&rqst_work_rqst);
      MPI_Request_free(&rqst_work_rqst);*/
  }
  if (work_rcvd_buf != NULL)
      safe_free(work_rcvd_buf);
  if ( msg != NULL)
      MsgIntBufferFree(msg);
  safe_free(mpi_rqst);
  safe_free(mpi_status);
  safe_free(done_indices);
  safe_free(grr_msg_buf);
  MPI_Type_free(&MPI_MATRIX_ROW);
  /** RANDOM_POLLING **/
  if (prog_args_struct->D_L_B == D_L_B_RANDOM_POLLING)
  {
      Cleanup_Random_Polling();
  }
  pthread_cond_destroy(&cond_worker_wait);
  pthread_mutex_destroy(&mutex_matrix);
```

```
    return error_status;
}
/*****************************************************************************
TokenRoutine:   Routine for processing the termination detection token.
*****************************************************************************/
void TokenRoutine( int my_rank, int group_size, int NO_WORK_THRESHOLD)
{
    int num_leaves, token_count, local_task_count;
    if ((NO_WORK_THRESHOLD > unsucc_work_attempts) ||
        (matrix_top_pos-matrix_cur_pos)+1 > 0 || token_received == FALSE ||
        expecting_reply != FALSE)
    {
        return;
    }
    if ( idle == FALSE )
    {
        token_count = 0;
        idle = TRUE;
    }
    else
    {
        token_count = token_count_buf + 1;
    }
    token_received = FALSE;
    if ( token_count == group_size )
    {
        num_leaves = group_size-1;
        MPI_Send(&num_leaves, 1, MPI_INT, my_rank, TAG_TERM, MPI_COMM_WORLD);
    }
    else
    {
        MPI_Send(&token_count, 1, MPI_INT, (my_rank +1)%group_size,
            TAG_TERM_TOKEN, MPI_COMM_WORLD);
    }
}
```

Appendix B: CODE FOR WORKER THREAD.

The **C** code for the woker thread as mentioned in Chapter 4.1.2. is listed in this appendix.

```
#include <stdlib.h>
#include <stdio.h>
#include <pthread.h>
#include <mpi.h>
#include <mpe.h>       /** MPI log facility **/
#include "prelim.h"
#include "prof.h"      /** profiling constants **/
#include  "defines.h"   /** const definitions for structs.h **/
#include  "structs.h"   /** aircraft struct definition **/
#include  "HSCTSearch.h"
#include  "lib.h"      /** matrix functions **/
#include "worker.h"
#include "random.h"
#include "grr_mc.h"
#include "compute.h"
#include "safemem.h"
/** Global variable used to coordinate token passing **/
extern int expecting_reply;
/*****************************************************************
WorkerRoutine:  Routine that performs low level analysis on
       local configurations, and waits for more work
       when all local configurations are analysed.
       This routine is also responsible for triggering the
       initial search for work.
*****************************************************************/
void WorkerRoutine( Worker_Args_Struct *worker_args)
{
   Aircraft *aircraft;
   int interval, j, target_node, flag, my_rank, group_size,
         *grr_msg_buf=NULL;
   MPI_Status work_rqst_status;
   MPI_Request rqst_work_rqst= MPI_REQUEST_NULL;
   VectorClass    point, point_copy; /*, flops_var;*/
   /** TASK COUNT TERMINATION **/
   int tasks_cmplt_count = 0, buf_tasks_cmplt = 0;
   MPI_Status status;
   MPI_Request tasks_cmplt_rqst = MPI_REQUEST_NULL;
   MPI_Comm_size( MPI_COMM_WORLD, &group_size);
   MPI_Comm_rank( MPI_COMM_WORLD, &my_rank);
   VectorClear( &point );
```

```
pthread_cleanup_push((void *)VectorClear,(void *)&point);
VectorNew(&point, tasks_matrix.nDim);
if ( point.d == NULL)
{
   fprintf(stderr, "worker(%d): cannot allocate point!\n",my_rank);
   pthread_exit(NULL);
}
pthread_cleanup_push((void *)VectorFree,(void *)&point);
VectorClear( &point_copy );
pthread_cleanup_push((void *)VectorClear,(void *)&point_copy);
VectorNew(&point_copy, tasks_matrix.nDim);
if ( point_copy.d == NULL)
{
   fprintf(stderr, "worker(%d): cannot allocate point_copy!\n",my_rank);
   pthread_exit(NULL);
}
pthread_cleanup_push((void *)VectorFree,(void *)&point_copy);
grr_msg_buf = safe_malloc(GRR_MC_MSG_SIZE*sizeof(int));
if ( grr_msg_buf == NULL)
{
   fprintf(stderr, "worker(%d): cannot allocate grr_msg_buf!\n",my_rank);
   pthread_exit(NULL);
}
pthread_cleanup_push((void *)safe_free,(void *)grr_msg_buf);
((Worker_Args_Struct *)worker_args)->aircraft->opt.des_var = point.d;
((Worker_Args_Struct *)worker_args)->aircraft->opt.num_dv =
      ((Worker_Args_Struct *)worker_args)->dvar->mDim;
if (worker_args->prog_args_struct->DO_LOG == TRUE)
   MPE_Log_event(COMPUTE_START, 0, M_COMPUTE_START);
while ( TRUE )
{
   pthread_mutex_lock(&mutex_matrix);
   pthread_cleanup_push((void *)pthread_mutex_unlock,(void *)&mutex_matrix);
      if ( termination != FALSE )
      {
         if (worker_args->prog_args_struct->DO_LOG == TRUE)
            MPE_Log_event(COMPUTE_END, 0, M_COMPUTE_END);
         pthread_exit(NULL);
      }
      /** if there are no more tasks left, dynamic load balncing is
         on, and no work request has been sent yet then send a
         request to a chosen node **/
      if ((matrix_top_pos-matrix_cur_pos)+1 <=
            worker_args->prog_args_struct->D_L_B_THRESHOLD
            && dlb == FALSE
            && worker_args->prog_args_struct->D_L_B != D_L_B_NONE )
```

```
{
   if (worker_args->prog_args_struct->D_L_B==D_L_B_RANDOM_POLLING)
   {
      /** RANDOM POLLING  **/
      target_node = Generate_Random_Node(my_rank, group_size);
      expecting_reply = TRUE;
      /** send work request to target node **/
      MPI_Test(&rqst_work_rqst, &flag, &status);
      MPI_Isend(NULL, 0, MPI_INT, target_node, TAG_WORK_RQST,
         MPI_COMM_WORLD, &rqst_work_rqst);
   }
   else if (worker_args->prog_args_struct->D_L_B
            == D_L_B_GRR_MC)
   {
      SendToParent(1, my_rank, 0, 1, (int**)&grr_msg_buf,
            &rqst_work_rqst);
   }
   dlb = TRUE;
}
while ( worker_args->prog_args_struct->D_L_B != D_L_B_NONE &&
      (matrix_top_pos-matrix_cur_pos)+1 == 0 )
{
   if ( worker_args->prog_args_struct->TERM == TERM_TASK_COUNT &&
      /** TASK COUNT TERMINATION  **/
         tasks_cmplt_count > 0 )
   {
      buf_tasks_cmplt = tasks_cmplt_count;
      MPI_Test(&rqst_work_rqst, &flag, &status);
      /** send message to manager node **/
      MPI_Isend(&buf_tasks_cmplt, 1, MPI_INT, MASTER_RANK,
         TAG_TERM_TASKS_CMPLT, MPI_COMM_WORLD, &tasks_cmplt_rqst);
      tasks_cmplt_count = 0 ;
   }
   /** TOKEN TERMINATION   **/
   if (worker_args->prog_args_struct->TERM == TERM_TOKEN)
   {
      TokenRoutine(my_rank, group_size,
         worker_args->prog_args_struct->NO_WORK_THRESHOLD);
   }
   if (worker_args->prog_args_struct->DO_LOG == TRUE)
      MPE_Log_event(IDLE_START, 0, M_IDLE_START);
   pthread_cond_wait(&cond_worker_wait,&mutex_matrix);
   if (worker_args->prog_args_struct->DO_LOG == TRUE)
      MPE_Log_event(IDLE_END, 0, M_IDLE_END);
   if ( termination != FALSE )
   {
```

```
            if (worker_args->prog_args_struct->DO_LOG == TRUE)
               MPE_Log_event(COMPUTE_END, 0, M_COMPUTE_END);
            pthread_exit(NULL);
         }
      }
      /** take one task **/
      /** copy current task to local scope **/
      memcpy(&point_copy.d[1],&tasks_matrix.d[matrix_cur_pos][1],
         tasks_matrix.nDim * sizeof(double));
      matrix_cur_pos++;
   pthread_mutex_unlock(&mutex_matrix);
   pthread_cleanup_pop(FALSE);
   /** do computation **/
   for ( j = 1; j <= worker_args->prog_args_struct->TASK_LENGTH; ++j)
   {
      VectorCopy(&point, &point_copy, FALSE);
      if ( LowFidelityAnalysis( ((Worker_Args_Struct *)worker_args)->cntrl,
         ((Worker_Args_Struct *)worker_args)->dvar, &point,
         ((Worker_Args_Struct *)worker_args)->aircraft,
            worker_args->prog_args_struct->PARTIAL_FACTORIAL_LEVELS) ==
            PRELIM_ERROR)
      {
         if (worker_args->prog_args_struct->DO_LOG == TRUE)
            MPE_Log_event(COMPUTE_END, 0, M_COMPUTE_END);
         pthread_exit(NULL);
      }
   }
   pthread_mutex_lock(&mutex_matrix);
      memcpy(&tasks_matrix.d[matrix_cur_pos-1][1], &point.d[1],
         tasks_matrix.nDim * sizeof(double));
   pthread_mutex_unlock(&mutex_matrix);
   if (worker_args->prog_args_struct->TERM == TERM_TASK_COUNT)
   {
      /** TASK COUNT TERMINATION  **/
      tasks_cmplt_count++;
   }
   if  (worker_args->prog_args_struct->D_L_B == D_L_B_NONE
         &&(matrix_top_pos-matrix_cur_pos)+1 == 0 )
   {
      termination = TRUE;
   }
} /** while (termination == FALSE) **/
MPI_Test(&tasks_cmplt_rqst, &flag, &status);
if ( flag == FALSE )
{
 /* MPI_Cancel(&tasks_cmplt_rqst);
```

```
      MPI_Request_free(&tasks_cmplt_rqst); */
   }
   MPI_Test(&rqst_work_rqst, &flag, &status);
   if ( flag == FALSE )
   {
    /* MPI_Cancel(&rqst_work_rqst);
      MPI_Request_free(&rqst_work_rqst); */
   }
   safe_free(grr_msg_buf);
   pthread_cleanup_pop(FALSE);
   VectorFree(&point_copy);
   pthread_cleanup_pop(FALSE);
   VectorClear(&point_copy);
   pthread_cleanup_pop(FALSE);
   VectorFree(&point);
   pthread_cleanup_pop(FALSE);
   VectorClear(&point);
   pthread_cleanup_pop(FALSE);
   if (worker_args->prog_args_struct->DO_LOG == TRUE)
   {
      MPE_Log_event(COMPUTE_END, 0, M_COMPUTE_END);
   }
}
```

Appendix C: CODE FOR GRR-MC THREAD.

The **C** code for the GRR-MC thread, and supporting routines as mentioned in Chapter 4.1.2. is listed in this appendix.

```
#include <stdio.h>
#include <errno.h>
#include <mpi.h>
#include <sys/timers.h>
#include <pthread.h>
#include "prelim.h"
#include "grr_mc.h"
#include "queue.h"
#include "safemem.h"
/** global variables **/
extern int termination;
/*******************************************************************************
SaveMsgFromParent:  Routine to save messages from GRR-MC parent node in GRR-MC
                message table.
*******************************************************************************/
int SaveMsgFromParent(int my_rank, int msg, int level)
{
   int *data = NULL;
   Q_Element *q_el;
   int parent_rank = -1;
   parent_rank = my_rank &  (1 << (level-1));
   data = (int *) safe_malloc(sizeof(int));
   if ( data == NULL )
   {
      fprintf(stderr, "SaveMsgFromParent(%d): cannot allocate data!\n",
         my_rank);
      return PRELIM_ERROR;
   }
   *data = msg;
   q_el = NULL;
   q_el = (Q_Element *) safe_malloc(sizeof(Q_Element));
   if ( q_el == NULL )
   {
      fprintf(stderr, "SaveMsgFromParent(%d): cannot allocate q_el!\n",
         my_rank);
      safe_free(data);
      return PRELIM_ERROR;
   }
   Init_Q_Element(q_el, (void *)data);
   pthread_mutex_lock(&mutex_grr_mc_msg_table);
```

```
      if ( my_rank == parent_rank &&
            glob_grr_mc_msg_table[level-2].from_parent.el_count > 0 )
      {
       fprintf(stderr, "SaveMsgFromParent(%d): glob_grr_mc_msg_table[%d].from_parent.el_count
%d > 0\n",
            my_rank, level-1, glob_grr_mc_msg_table[level-1].from_left);
         safe_free(q_el);
         safe_free(data);
         return PRELIM_ERROR;
      }
      Join_Q(&glob_grr_mc_msg_table[level-2].from_parent, q_el);
      glob_is_grr_mc_msg_table_dirty = TRUE;
   pthread_mutex_unlock(&mutex_grr_mc_msg_table);
   return PRELIM_SUCCESS;
}
/*****************************************************************************
SaveMsgFromLeft:    Routine to save messages from GRR-MC left child node in GRR-MC
                message table.
*****************************************************************************/
int SaveMsgFromLeft(int my_rank, int msg, int level)
{
   pthread_mutex_lock(&mutex_grr_mc_msg_table);
      if ( glob_grr_mc_msg_table[level].from_left != 0 )
      {
         fprintf(stderr, "SaveMsgFromLeft(%d): glob_grr_mc_msg_table[%d].from_left %d != 0\n",
          my_rank, level, glob_grr_mc_msg_table[level].from_left);
          return PRELIM_ERROR;
      }
      glob_grr_mc_msg_table[level].from_left = msg;
      glob_is_grr_mc_msg_table_dirty = TRUE;
   pthread_mutex_unlock(&mutex_grr_mc_msg_table);
   return PRELIM_SUCCESS;
}
/*****************************************************************************
SaveMsgFromRight:   Routine to save message from GRR-MC right child node in GRR-MC
                message table.
*****************************************************************************/
int SaveMsgFromRight(int my_rank, int msg, int level)
{
   int *data = NULL;
   Q_Element *q_el;
   data = (int *) safe_malloc(sizeof(int));
   if ( data == NULL )
   {
      fprintf(stderr, "SaveMsgFromRight(%d): cannot allocate data!\n",
         my_rank);
```

```
        return PRELIM_ERROR;
    }
    *data = msg;
    q_el = NULL;
    q_el = (Q_Element *) safe_malloc(sizeof(Q_Element));
    if ( q_el == NULL )
    {
        fprintf(stderr, "SaveMsgFromRight(%d): cannot allocate q_el!\n",
            my_rank);
        safe_free(data);
        safe_free(q_el);
        return PRELIM_ERROR;
    }
    Init_Q_Element(q_el, (void *)data);
    pthread_mutex_lock(&mutex_grr_mc_msg_table);
        Join_Q(&glob_grr_mc_msg_table[level].from_right, q_el);
        glob_is_grr_mc_msg_table_dirty = TRUE;
    pthread_mutex_unlock(&mutex_grr_mc_msg_table);
    return PRELIM_SUCCESS;
}
/*****************************************************************************
InitGRRRecvs:   Routine that initiatlizes the persistent MPI recieve requests for all
             GRR-MC messages.
*****************************************************************************/
void InitGRRRecvs(int my_rank, int group_size, MPI_Request *mpi_rqst,
    int **msg, int offset, int total_msgs)
{
    /** Initialize persistent receive requests needed by the GRR-MC **/
    int tree_height = 0, subtree_height = 0, i = 0,
        rank = -1, local_offset = 0;
    /** calculate the spanning tree height **/
    for ( tree_height=1; ((group_size-1) >> tree_height)!= 0; ++tree_height);
    /** calculate the height of the tallest subtree that this node
      is the root of.
     **/
    for (subtree_height=0;((my_rank >> subtree_height) & 1)==0 &&
        subtree_height < tree_height; ++subtree_height);
    local_offset = offset;
    /** receive the target **/
    MPI_Recv_init( msg[0], 1, MPI_INT, MPI_ANY_SOURCE,
        TAG_GRR_MC_TARGET, MPI_COMM_WORLD, &mpi_rqst[local_offset]);
    local_offset++;
    /** receive reply from parent of node's subtree, if any **/
    if (subtree_height > 0 && subtree_height < tree_height)
    {
        rank = my_rank &  (1 << subtree_height);
```

```
        MPI_Recv_init(msg[1], GRR_MC_MSG_SIZE, MPI_INT, rank,
            TAG_GRR_MC_TARGET_REPLY, MPI_COMM_WORLD, &mpi_rqst[local_offset]);
        local_offset++;
    }
    /** receive messages only from child nodes that exist **/
    for (i=0 ; i+local_offset < total_msgs; i++)
    {
        rank = (unsigned int)my_rank | (1 << i);
        if ( rank < group_size )
        {
            MPI_Recv_init(msg[i+local_offset-offset], GRR_MC_MSG_SIZE, MPI_INT, rank,
                TAG_GRR_MC_TARGET_RQST, MPI_COMM_WORLD,
                &mpi_rqst[i+local_offset]);
        }
    }
    MPI_Startall(total_msgs-offset, mpi_rqst+offset);
}
/*****************************************************************************
GetGRRMessageCount: Routine to calculate the total amount of GRR-MC messages that
                this node will be receiving from other nodes.
*****************************************************************************/
int GetGRRMessageCount(int my_rank, int group_size)
{
    int tree_height = 0, subtree_height = 0, i = 0, total_msgs = 0;
    /** calculate the spanning tree height **/
    for ( tree_height=1; ((group_size-1) >> tree_height) != 0; ++tree_height);
    /** calculate the height of the tallest subtree that this node
      is the root of.
     **/
    for (subtree_height=0;((my_rank >> subtree_height) & 1)==0 &&
           subtree_height < tree_height; ++subtree_height);
    /** the first one is for receiving the TARGET **/
    total_msgs = 1;
    /** add the messages from existing children **/
    for (i = 0; i<subtree_height; ++i)
    {
        if ((my_rank | (1 << i)) < group_size)
            total_msgs++;
    }
    /** add message from parent of subtree, if it exists **/
    if ( subtree_height > 0 && subtree_height < tree_height )
        total_msgs++;
    return total_msgs;
}
/*****************************************************************************
GRR_MC_Routine: Routine that sleeps for a specified delay time and then processed all
```

```
            GRR-MC messages that have accumulated in the message table.
*******************************************************************************/
void GRR_MC_Routine(GRR_MC_Args_Struct *grr_mc_args)
{
    register int i;
    TreeLvlMsg *msg_table = NULL;
    Queue *request_q = NULL;
    int target = 0, group_size, my_rank, rqst_pool_size,
           subtree_height = 0, tree_height = 0;
    Q_Element *q_el = NULL;
    TreeLvlRqst *rqst = NULL;
    struct timespec sleep_time;
    pthread_mutex_t mutex;
    pthread_cond_t cond;
    unsigned long tot_wait_time;
    Clear_Q_Params param;
    /** message and request buffers **/
    int **msg_buf = NULL;
    MPI_Request *mpi_rqst_pool = NULL;
    MPI_Comm_size( MPI_COMM_WORLD, &group_size);
    MPI_Comm_rank( MPI_COMM_WORLD, &my_rank);
    pthread_cond_init(&cond,pthread_condattr_default);
    pthread_cleanup_push((void *)pthread_cond_destroy,(void *)&cond);
    pthread_mutex_init(&mutex_grr_mc_msg_table, pthread_mutexattr_default);
    pthread_cleanup_push((void *)pthread_mutex_destroy,
           (void *)&mutex_grr_mc_msg_table);
    pthread_mutex_init(&mutex, pthread_mutexattr_default);
    pthread_cleanup_push((void *)pthread_mutex_destroy,(void *)&mutex);
    /** calculate the spanning tree height **/
    for ( tree_height=1; ((group_size-1) >> tree_height) != 0; ++tree_height);
    /** calculate the height of the tallest subtree of the GRR-MC spanning tree
       that this node is the root of.
     **/
    for (subtree_height=0;((my_rank >> subtree_height) & 1)==0 &&
           subtree_height < tree_height; ++subtree_height);
    /** allocate message and memory buffers **/
    rqst_pool_size = 10*(subtree_height+1);
    msg_buf = MsgIntBufferCreate(my_rank, rqst_pool_size, GRR_MC_MSG_SIZE);
    if ( msg_buf == NULL )
    {
       fprintf(stderr, "GRR_MC_Routine(%d): cannot allocate msg_buf!\n",
              my_rank);
       pthread_exit(NULL);
    }
    pthread_cleanup_push((void *)MsgIntBufferFree,(void *)msg_buf);
    mpi_rqst_pool = (MPI_Request *)safe_calloc(rqst_pool_size, sizeof(MPI_Request));
```

```
if ( mpi_rqst_pool == NULL)
{
   fprintf(stderr, "GRR_MC_Routine(%d): cannot allocate mpi_rqst_pool!\n",
          my_rank);
   pthread_exit(NULL);
}
pthread_cleanup_push((void *)safe_free,(void *)mpi_rqst_pool);
for (i = 0; i < rqst_pool_size; i++)
{
   mpi_rqst_pool[i] = MPI_REQUEST_NULL;
}
glob_is_grr_mc_msg_table_dirty = FALSE;
glob_grr_mc_msg_table =
      (TreeLvlMsgQ *) safe_calloc(subtree_height, sizeof(TreeLvlMsgQ));
if ( glob_grr_mc_msg_table == NULL )
{
   fprintf(stderr, "GRR_MC_Routine(%d): cannot allocate glob_grr_mc_msg_table!\n",
          my_rank);
   pthread_exit(NULL);
}
pthread_cleanup_push((void *)safe_free,(void *)glob_grr_mc_msg_table);
/** allocate a vector that stores a queue of immediate child requests
   for each level of the spanning tree that this node is a member of,
   except for the leaf level.
 **/
request_q =   (Queue *) safe_calloc(subtree_height, sizeof(Queue));
if ( request_q == NULL )
{
   fprintf(stderr, "GRR_MC_Routine(%d): cannot allocate request_q!\n",
          my_rank);
   pthread_exit(NULL);
}
pthread_cleanup_push((void *)safe_free,(void *)request_q);
/** initialize the queue at every level **/
for (i = 0; i<subtree_height; i++)
{
   Init_Q(&request_q[i]);
   Init_Q(&glob_grr_mc_msg_table[i].from_parent);
   glob_grr_mc_msg_table[i].from_left = 0;
   Init_Q(&glob_grr_mc_msg_table[i].from_right);
}
param.subtree_height = subtree_height;
param.request_q = request_q;
param.glob_grr_mc_msg_table = glob_grr_mc_msg_table;
pthread_cleanup_push((void *)Clear_Qs,(void *)&param);
/** allocate a table containing this node's parent and two children
```

```
   for every level of the spanning tree that the node is at,
   except for the leaf level.
 **/
msg_table = (TreeLvlMsg *) safe_calloc(subtree_height, sizeof(TreeLvlMsg));
if ( msg_table== NULL )
{
   fprintf(stderr, "GRR_MC_Routine(%d): cannot allocate msg_table!\n",
         my_rank);
   pthread_exit(NULL);
}
pthread_cleanup_push((void *)safe_free,(void *)msg_table);
while(termination == FALSE)
{
   /** this loop implements buzy waiting, by sleeping for the
      required amount of time by the GRR-MC specs, and then
      processing all messages that have been received for
      that period.
   **/
   if (grr_mc_args->grr_mc_delay > 0 )
   {
      tot_wait_time = grr_mc_args->grr_mc_delay *
         (unsigned long)(MPI_Wtick() * 1e9);
      getclock(TIMEOFDAY, &sleep_time);
      sleep_time.tv_nsec = sleep_time.tv_nsec +
         (tot_wait_time % (unsigned long)1e9);
      sleep_time.tv_sec = sleep_time.tv_sec +
         (tot_wait_time / 1e9);
      pthread_mutex_lock(&mutex);
         pthread_cond_timedwait(&cond, &mutex, &sleep_time);
      pthread_mutex_unlock(&mutex);
   }
   /** if any new messages have arrived make a snapshot of the global GRR-MC
      messages table, and reset it to empty status, otherwise go back to
      sleep for the specified number of seconds.
    **/
   pthread_mutex_lock(&mutex_grr_mc_msg_table);
      if (glob_is_grr_mc_msg_table_dirty == FALSE  )
      {
         pthread_mutex_unlock(&mutex_grr_mc_msg_table);
         pthread_yield();
         continue;
      }
      for (i = 0; i < subtree_height; i++)
      {
         if ( glob_grr_mc_msg_table[i].from_parent.el_count > 0)
         {
```

```
                q_el = Pop_Q(&glob_grr_mc_msg_table[i].from_parent);
                msg_table[i].from_parent =  *(int *)q_el->data;
                Destroy_Q_Element(q_el);
            }
            else
            {
                msg_table[i].from_parent = MSG_NONE;
            }
            msg_table[i].from_left = glob_grr_mc_msg_table[i].from_left;
            glob_grr_mc_msg_table[i].from_left = 0;
            if (glob_grr_mc_msg_table[i].from_right.el_count > 0)
            {
                q_el = Pop_Q(&glob_grr_mc_msg_table[i].from_right);
                msg_table[i].from_right =  *(int *)q_el->data;
                Destroy_Q_Element(q_el);
            }
            else
            {
                msg_table[i].from_right =  0;
            }
            if (glob_grr_mc_msg_table[i].from_parent.el_count == 0 &&
                glob_grr_mc_msg_table[i].from_right.el_count == 0)
                glob_is_grr_mc_msg_table_dirty = FALSE;
        }
    pthread_mutex_unlock(&mutex_grr_mc_msg_table);
    /** for all levels that this node belongs to process the
        messages starting from the lowest level
     **/
    for ( i = 0; i < subtree_height && (termination == FALSE); i++)
    {
        /** handle messages from parent node, if any, and if this is not the
            global root level.
         **/
        if  ( msg_table[i].from_parent > MSG_NONE )
        {
            if ( i >= (tree_height-1) )
                fprintf(stderr, "GRR_MC_Routine(%d): root has message from parent %d\n",
                       my_rank, msg_table[i].from_parent);
            if (request_q[i].el_count == 0)
            {
                fprintf(stderr, "GRR_MC_Routine(%d): request q at level %d gets reply with no
rqsts\n",
                   my_rank, i+1);
                pthread_exit(NULL);
            }
            else
```

```
        q_el = Pop_Q(&request_q[i]);
    if ( SendToChildren(((TreeLvlRqst *)q_el->data)->left_rqst,
            ((TreeLvlRqst *)q_el->data)->right_rqst,
            msg_table[i].from_parent, my_rank, group_size, i+1,
            rqst_pool_size, msg_buf, mpi_rqst_pool)
            == PRELIM_ERROR)
    {
        Destroy_Q_Element(q_el);
        pthread_exit(NULL);
    }
    Destroy_Q_Element(q_el);
}
/** handle messages from child nodes, if any **/
if  ( (msg_table[i].from_left + msg_table[i].from_right) > 0 )
{
    if ( i == (tree_height - 1))
    {
        if (SendToChildren( msg_table[i].from_left, msg_table[i].from_right,
            target, my_rank, group_size, i+1,
            rqst_pool_size, msg_buf, mpi_rqst_pool)==PRELIM_ERROR)
        {
            pthread_exit(NULL);
        }
        target += msg_table[i].from_left + msg_table[i].from_right;
        target %= group_size;
    }
    else
    {
        rqst = NULL;
        rqst = (TreeLvlRqst *) safe_malloc(sizeof(TreeLvlRqst));
        if( rqst == NULL )
        {
            fprintf(stderr, "GRR_MC_Routine(%d): cannot allocate rqst, i %d\n",
                my_rank, i);
            pthread_exit(NULL);
        }
        rqst->left_rqst = msg_table[i].from_left;
        rqst->right_rqst = msg_table[i].from_right;
        q_el = NULL;
        q_el = (Q_Element *) safe_malloc(sizeof(Q_Element));
        if( q_el == NULL )
        {
            fprintf(stderr, "GRR_MC_Routine(%d): cannot allocate q_el, i %d\n",
                my_rank, i);
            pthread_exit(NULL);
        }
```

```
                Init_Q_Element(q_el, rqst);
                Join_Q( &request_q[i], q_el);
                if (SendToParent(msg_table[i].from_left+msg_table[i].from_right,
                   my_rank, i+1, rqst_pool_size, msg_buf, mpi_rqst_pool)
                      == PRELIM_ERROR)
                {
                   pthread_exit(NULL);
                }
             }
          }
       }
    }
    /** cleanup **/
    safe_free(msg_table);
    pthread_cleanup_pop(FALSE);
    Clear_Qs(&param);
    pthread_cleanup_pop(FALSE);
    safe_free(request_q);
    pthread_cleanup_pop(FALSE);
    safe_free(glob_grr_mc_msg_table);
    pthread_cleanup_pop(FALSE);
    safe_free(mpi_rqst_pool);
    pthread_cleanup_pop(FALSE);
    MsgIntBufferFree(msg_buf);
    pthread_cleanup_pop(FALSE);
    pthread_mutex_destroy,(&mutex);
    pthread_cleanup_pop(FALSE);
    pthread_mutex_destroy(&mutex_grr_mc_msg_table);
    pthread_cleanup_pop(FALSE);
    pthread_cond_destroy(&cond);
    pthread_cleanup_pop(FALSE);
}
/*****************************************************************************
SendToParent:   Send a message to GRR-MC parent node.
*****************************************************************************/
int SendToParent(int msg_from_child,  int my_rank, int cur_level,
       int rqst_pool_size, int **msg_buf, MPI_Request *mpi_rqst_pool)
{
    MPI_Status mpi_status;
    int parent_rank = -1, test_flag = FALSE, i = 0, index = MPI_UNDEFINED;
    parent_rank = my_rank &  (1 << cur_level);
    if (parent_rank == my_rank )
    {
       if( SaveMsgFromLeft(my_rank, msg_from_child, cur_level) == PRELIM_ERROR)
          return PRELIM_ERROR;
    }
```

```
    else
    {
       test_flag = FALSE;
       for ( i=0;(i<1000)&&(termination==FALSE)&&(test_flag == FALSE)&&
             (rqst_pool_size > 0);i++)
       {
          MPI_Testany( rqst_pool_size, mpi_rqst_pool, &index,
             &test_flag, &mpi_status);
          pthread_yield();
       }
       if ( test_flag == FALSE || rqst_pool_size == 0)
       {
         fprintf(stderr, "SendToParent(%d): Target reply cannot be sent, term %d, rqst_pool_size
%d!\n",
             my_rank, termination, rqst_pool_size);
          return PRELIM_ERROR;
       }
       if (index == MPI_UNDEFINED)
          index= 0;
       msg_buf[index][0] = msg_from_child;
       msg_buf[index][1] = cur_level;
       MPI_Isend(msg_buf[index], 2, MPI_INT, parent_rank, TAG_GRR_MC_TARGET_RQST,
           MPI_COMM_WORLD, &mpi_rqst_pool[index]);
    }
    return PRELIM_SUCCESS;
}
/*****************************************************************************
SendToChildren: Send messages to GRR-MC child nodes.
*****************************************************************************/
int SendToChildren( int left_child_rqst, int right_child_rqst,
       int msg_from_parent, int my_rank, int group_size, int cur_level,
       int rqst_pool_size, int **msg_buf, MPI_Request *mpi_rqst_pool)
{
    MPI_Status mpi_status;
    int left_child_rank = -1, right_child_rank = -1, return_value,
       test_flag = FALSE, i = 0, index = MPI_UNDEFINED, *data = NULL;
    Q_Element *q_el = NULL;
    return_value = PRELIM_SUCCESS;
    left_child_rank = my_rank;
    right_child_rank = ((unsigned int)my_rank) | (1 << (cur_level-1));
    if (cur_level == 1)
    {
       if (left_child_rqst > 0)
       {
          test_flag = FALSE;
          for ( i=0;(i<1000)&&(termination==FALSE)&&(test_flag == FALSE)&&
```

```
            (rqst_pool_size > 0);i++)
        {
            MPI_Testany( rqst_pool_size, mpi_rqst_pool, &index,
                &test_flag, &mpi_status);
            pthread_yield();
        }
        if ( test_flag == FALSE || rqst_pool_size == 0)
        {
            fprintf(stderr, "SendToChildren(%d): taget to left child cannot be sent!\n",
                my_rank);
            return PRELIM_ERROR;
        }
        if (index == MPI_UNDEFINED)
            index= 0;
        msg_buf[index][0] = msg_from_parent;
        MPI_Isend(msg_buf[index], 1, MPI_INT, left_child_rank,
            TAG_GRR_MC_TARGET, MPI_COMM_WORLD, &mpi_rqst_pool[index]);
    }
    if (right_child_rqst > 0)
    {
        test_flag = FALSE;
        for ( i=0;(i<1000)&&(termination==FALSE)&&(test_flag == FALSE)&&
            (rqst_pool_size > 0);i++)
        {
            MPI_Testany( rqst_pool_size, mpi_rqst_pool, &index,
                &test_flag, &mpi_status);
            pthread_yield();
        }
        if ( test_flag == FALSE || rqst_pool_size == 0)
        {
            fprintf(stderr, "SendToChildren(%d): taget to right child cannot be sent!\n",
                my_rank);
            return PRELIM_ERROR;
        }
        if (index == MPI_UNDEFINED)
            index= 0;
        msg_buf[index][0] = msg_from_parent + left_child_rqst;
        msg_buf[index][0] %= group_size;
        MPI_Isend(msg_buf[index], 1, MPI_INT, right_child_rank,
            TAG_GRR_MC_TARGET, MPI_COMM_WORLD, &mpi_rqst_pool[index]);
    }
}
else
{
    if (left_child_rqst > 0)
    {
```

```
            if ( SaveMsgFromParent(my_rank, msg_from_parent, cur_level) ==
                   PRELIM_ERROR)
               return PRELIM_ERROR;
         }
         if ( right_child_rqst> 0)
         {
            test_flag = FALSE;
            for ( i=0;(i<1000)&&(termination==FALSE)&&(test_flag == FALSE)&&
               (rqst_pool_size > 0);i++)
            {
               MPI_Testany( rqst_pool_size, mpi_rqst_pool, &index,
                  &test_flag, &mpi_status);
               pthread_yield();
            }
            if ( test_flag == FALSE || rqst_pool_size == 0)
            {
               fprintf(stderr,"SendToChildren(%d): cannot send to right!\n",
                  my_rank);
               return PRELIM_ERROR;
            }
            if (index == MPI_UNDEFINED)
               index= 0;
            msg_buf[index][0] = left_child_rqst + msg_from_parent;
            msg_buf[index][0] %= group_size;
            msg_buf[index][1] = cur_level;
            i = MPI_Isend(msg_buf[index], 2, MPI_INT, right_child_rank,
               TAG_GRR_MC_TARGET_REPLY, MPI_COMM_WORLD, &mpi_rqst_pool[index]);
         }
      }
      return return_value;
}
```

Appendix D: DESIGN VARIABLE DEFINITION FILE USED FOR TEST RUNS.

This is a listing of the design variable definition file used for all test runs described in this thesis. The file specifies nominal values, scaling factors and move limits for all 29 design variables.

```
#Design variables after cycle  0
#29          Number of design variables
1 1.64096261431  0.90    1.10      1)  x100, wing root chord (ft.)
2 1.02408973683  0.90    1.10      2)  x100, L.E. break, x (ft.)
3 3.45162853760  0.90    1.10      3)   x10, L.E. break, y (ft.)
4 1.48328698215  0.95    1.05      4)  x100, T.E. break, x (ft.)
5 2.63225104343  0.95    1.15      5)   x10, T.E. break, y (ft.)
6 1.29115031424  0.95    1.15      6)  x100, L.E. wing tip, x (ft.)
7 1.09276364577  0.90    1.10      7)   x10, wing tip chord (ft.)
8 7.02892196451  0.90    1.10      8)   x10, wing semi-span (ft.)
9 4.95664234483  0.90    1.10      9)  x0.1, location of max. t/c on airfoil (x/c)
10 3.22302689070  0.90    1.10     10)    x1, L.E. radius parameter
11 3.00807173152  0.90    1.10     11) x0.01, t/c at wing root
12 2.11606696299  0.90    1.10     12) x0.01, t/c at L.E. break 1
13 1.83790866614  0.90    1.10     13) x0.01, t/c at wing tip
14 0.22780937915  0.90    1.15     14)  x100, fuselage restraint 1, x (ft.)
15 0.35754528327  0.90    1.10     15)   x10, fuselage restraint 1, r (ft.)
16 1.13290732737  0.85    1.15     16)  x100, fuselage restraint 2, x (ft.)
17 0.49449630510  0.95    1.05     17)   x10, fuselage restraint 2, r (ft.)
18 1.29314680446  0.85    1.15     18)  x100, fuselage restraint 3, x (ft.)
19 0.47098654714  0.95    1.05     19)   x10, fuselage restraint 3, r (ft.)
20 2.03776220420  0.90    1.15     20)  x100, fuselage restraint 4, x (ft.)
21 0.56988572208  0.95    1.05     21)   x10, fuselage restraint 4, r (ft.)
22 1.01430224591  0.95    1.15     22)   x10, nacelle 1 y location (ft.)
23 1.95367015459  0.85    1.05     23)   x10, nacelle 2 y location (ft.)
24 4.08559941655  0.95    1.05     24) x1e05, flight fuel (lbs.)
25 5.65244506717  0.90    1.10     25) x1e04, starting cruise altitude (ft.)
26 0.39716110063  0.90    1.10     26)  x100, cruise climb rate (ft./min.)
27 5.64621807013  0.90    1.10     27)  x100, vertical tail area
28 8.23320534848  0.90    1.10     28)  x100, horizontal tail area
29 4.60000000000  0.90    1.10     29) x1000, thrust (lbs)
```

VITA.

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